



Supplement of

Tropical tree height and crown allometries for the Barro Colorado Nature Monument, Panama: a comparison of alternative hierarchical models incorporating interspecific variation in relation to life history traits

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Table S3. Parameter estimates for all the hierarchical models for tree height allometry.

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Figure S1. Tree height allometry for the 162 species analyzed, showing observations and fitted relationships.

Figure S2. Crown area allometry for the 162 species analyzed, showing observations and fitted relationships.

Figure S3. Extended version of Figure 4 in the main text showing the entire range of observed DBHs.

References

Section S2. Stan code used to fit alternative allometric models.

Table S1. Sources of field measurement data for tree heights and crown dimensions, methods, site of measurement and the number of data points. Where crown areas were not measured directly, they were estimated as pi times the geometric mean crown radius. Where two height measurement methods are listed, the telescoping pole was used on small individuals and the other method on larger individuals.

Source (name)	Crown method	Height method	Site	Years	N Crowns	N Heights	Observers	Reference
1 O'Brien (<i>O'BrienBCI1993</i>)	8 radii ¹	Telescoping pole ² or tangent method ³	BCI	1993	171	171	S. O'Brien	O'Brien et al. 1995
2 Spiro (<i>SpiroBCI1993</i>)	8 radii ¹	Telescoping pole ² or tangent method ³	BCI	1993	195	194	Spiro	Bohlman & O'Brien 2006
3 Thomas (<i>ThomasBCI2000</i>)	–	Telescoping pole ² or tangent method ³	BCI	2000	–	43	Thomas	Thomas (unpubl data)
4 Bohlman (<i>BohlmanBCI1997</i>)	8 radii ¹	Sine method ⁴	BCI	1997	175	182	S. A. Bohlman	Bohlman & O'Brien 2006
5 Wright (<i>WrightBCI2007</i>)	8 radii ¹	Telescoping pole ² or tangent method ³	BCI	2007	760	824	M. C. Ruiz-Jaen & C. Salvador	Wright et al. 2010
6 Wright (<i>WrightGigante1998</i>)	–	Telescoping pole ² or tangent method ³	Gigante	1998-1999	–	4720	A. Peterson, C. Korine, O. Hernandez & R. Gonzalez	NA
7 Muller-Landau (<i>MullerLandauBCI1996</i>)	Longest diameter and perpendicular diameter ⁵	Telescoping pole ²	BCI	1996-1999	505	1019	H. Muller-Landau	NA
8 Muller-Landau (<i>MullerLandauBCI2000</i>)	–	Telescoping pole ² or sine method ⁴	BCI	–	–	2113	P. Ramos, P. Villareal	NA
9 Muller-Landau (<i>MullerLandauBCI2014</i>)	Photogrammetry ⁶	Photogrammetry minus lidar DEM ⁷	BCI	2014	619	619	J. Dandois	NA
<i>Total</i>					2425	9885		

¹ The horizontal distance from the trunk to the vertical projection of the edge of the canopy was measured in eight compass directions 45 degrees apart, including magnetic north.

² Height measurements were made with a height-marked telescoping pole for individuals that could be reached by this pole (typically to 5 or 8 m height).

³ The tangent method involves combining measurements of the angle to the top of the tree and the distance to the base of the tree and calculating height as the distance times the tangent of the angle, with corrections for the height of the observer relative to the base of the tree (see Larjavaara & Muller-Landau 2013). In early studies, the distance to the base of the tree was measured manually; in later studies, with a laser rangefinder.

⁴ The sine method is based on measuring the distance to the highest leaf using a laser rangefinder and the angle of that measurement relative to horizontal, and calculating the height as the distance times the sine of the angle (note that the sine is 1 if the measurement is completely vertical), with corrections for the height of the observer relative to the base of the tree (see Larjavaara & Muller-Landau 2013 for details). Modern laser rangefinder models for forestry applications often return the vertical distance directly.

⁵ The horizontal distance spanning the longest dimension of the crown was measured together with the perpendicular horizontal dimension of the crown at its widest point.

⁶ Overlapping aerial photos taken by an unmanned aerial vehicle in October 2014 were processed using Agisoft Photoscan to obtain a 3D point cloud, from which orthomosaics and canopy surface elevation maps were produced at a resolution of 7 cm (Dandois & Ellis 2013; Graves et al. 2018). The orthomosaic and canopy surface maps were georeferenced by comparison with 2009 1-m resolution airborne lidar data. Individual tree crowns greater than 50 m² in area were manually delineated, and were assigned to tagged trees in the 50 ha forest dynamics plot through ground-based field work that also assessed whether they were fully sun-exposed. For fully sun-exposed individuals, crown area was estimated as the area of the delineated crown.

⁷ A 1-m ground digital elevation model from airborne LiDAR (2009) was subtracted from the canopy surface elevation calculated from the aerial photos as above to obtain a map of canopy height across the 50 ha plot. For each delineated crown linked to a tagged, fully sun-exposed tree, tree height was assessed as the maximum canopy height within the delineated crown area.

Table S2. Posterior, species-level parameter estimates (median and 90% posterior interval) for predicting tree height (m) and crown area (m^2) from trunk diameter (cm) for the focal species. Unbiased estimates of tree height and crown area can be obtained by multiplying the values predicted by these equations by 1.017 in the case of heights, and 1.163 for crown area, to correct for the bias from back-transforming predicted values of log height and log crown area (Sprugel, 1983). Species taxonomy and mnemonics according to Condit et al. (2017).

Mnemonic	Species	Tree height (generalized Michaelis-Menten, Eq. 3)			Crown area (power function, Eq. 2)	
		a	b	k	a	b
ade1tr	<i>Adelia triloba</i>	57.1 (48.1, 67.9)	0.66 (0.55, 0.77)	23.2 (17.7, 29.1)	0.800 (0.371, 1.783)	1.34 (1.07, 1.60)
alchco	<i>Alchornea costaricensis</i>	53.0 (44.4, 63.3)	0.64 (0.57, 0.72)	18.8 (15.0, 23.2)	0.553 (0.255, 1.203)	1.33 (1.11, 1.55)
allops	<i>Allophylus psilospermus</i>	57.9 (48.9, 69.0)	0.74 (0.63, 0.85)	22.0 (16.6, 28.0)	0.660 (0.302, 1.415)	1.35 (1.10, 1.62)
alsebl	<i>Alseis blackiana</i>	56.2 (48.6, 65.0)	0.73 (0.71, 0.77)	21.7 (18.8, 25.0)	0.228 (0.195, 0.265)	1.49 (1.42, 1.54)
amaico	<i>Amaoua corymbosa</i>	63.0 (53.0, 75.3)	0.70 (0.62, 0.77)	20.7 (16.9, 25.3)	0.721 (0.378, 1.452)	1.30 (1.04, 1.53)
anacex	<i>Anacardium excelsum</i>	48.5 (42.8, 56.3)	0.82 (0.70, 0.95)	17.6 (11.1, 24.3)	0.611 (0.262, 1.387)	1.32 (1.15, 1.50)
andiin	<i>Andira inermis</i>	63.5 (53.6, 75.5)	0.74 (0.64, 0.84)	24.6 (18.7, 31.0)	0.444 (0.187, 1.051)	1.38 (1.12, 1.64)
annoac	<i>Annona acuminata</i>	62.2 (52.1, 74.5)	0.72 (0.59, 0.84)	23.5 (18.0, 29.4)	0.669 (0.364, 1.258)	1.32 (1.08, 1.55)
apeime	<i>Apeiba membranacea</i>	53.9 (46.2, 62.9)	0.71 (0.65, 0.78)	18.5 (15.6, 21.6)	0.997 (0.454, 2.338)	1.15 (0.95, 1.34)
apeiti	<i>Apeiba tibourbou</i>	42.5 (34.5, 52.3)	0.78 (0.65, 0.90)	18.7 (12.9, 25.3)	0.562 (0.239, 1.299)	1.34 (1.09, 1.59)
ardife	<i>Ardisia standleyana</i>	62.3 (52.3, 74.2)	0.62 (0.53, 0.72)	22.4 (17.9, 27.3)	0.737 (0.380, 1.415)	1.32 (1.07, 1.55)
aspicr	<i>Aspidosperma desmanthum</i>	62.5 (54.6, 72.4)	0.77 (0.72, 0.82)	19.6 (17.2, 22.5)	0.692 (0.328, 1.515)	1.24 (1.05, 1.42)
ast2gr	<i>Astronium graveolens</i>	63.9 (55.3, 74.9)	0.79 (0.72, 0.85)	23.7 (19.8, 28.1)	0.578 (0.234, 1.282)	1.30 (1.09, 1.53)
beilpe	<i>Beilschmiedia tovarensis</i>	52.4 (47.2, 58.4)	0.91 (0.88, 0.95)	26.9 (24.2, 30.1)	0.583 (0.500, 0.677)	1.27 (1.21, 1.33)
brosal	<i>Brosimum alicastrum</i>	63.2 (56.4, 71.2)	0.80 (0.77, 0.84)	29.4 (26.5, 32.9)	0.939 (0.795, 1.116)	1.28 (1.22, 1.33)
brosgu	<i>Brosimum guianense</i>	62.0 (52.5, 73.6)	0.71 (0.64, 0.78)	19.6 (16.2, 23.5)	0.790 (0.458, 1.364)	1.30 (1.10, 1.51)
calolo	<i>Calophyllum longifolium</i>	61.1 (53.3, 71.0)	0.74 (0.69, 0.79)	20.7 (17.8, 24.1)	0.495 (0.267, 0.911)	1.37 (1.22, 1.52)
caseac	<i>Casearia aculeata</i>	61.7 (52.1, 73.4)	0.74 (0.63, 0.85)	23.1 (17.6, 29.0)	0.603 (0.302, 1.189)	1.34 (1.09, 1.57)
casear	<i>Casearia arborea</i>	56.4 (47.1, 68.3)	0.67 (0.59, 0.76)	17.3 (13.5, 21.9)	0.624 (0.262, 1.473)	1.29 (1.06, 1.53)
casesy	<i>Casearia sylvestris</i>	57.7 (48.4, 68.4)	0.69 (0.58, 0.79)	22.6 (16.7, 28.9)	0.594 (0.262, 1.389)	1.34 (1.10, 1.60)
cassel	<i>Cassipourea elliptica</i>	59.9 (51.2, 70.4)	0.74 (0.69, 0.80)	23.5 (19.7, 27.9)	0.536 (0.313, 0.908)	1.39 (1.21, 1.56)
cavapl	<i>Cavanillesia platanifolia</i>	51.7 (45.5, 60.2)	0.77 (0.68, 0.87)	16.9 (12.5, 22.0)	0.524 (0.220, 1.245)	1.21 (1.04, 1.39)
cecrin	<i>Cecropia insignis</i>	47.1 (41.6, 54.1)	0.96 (0.90, 1.03)	22.9 (20.3, 25.9)	0.254 (0.195, 0.328)	1.65 (1.56, 1.75)
cecrob	<i>Cecropia obtusifolia</i>	40.1 (32.3, 50.2)	0.88 (0.71, 1.05)	12.4 (7.1, 18.8)	0.665 (0.304, 1.678)	1.20 (0.93, 1.44)
ceibpe	<i>Ceiba pentandra</i>	53.6 (48.1, 60.7)	0.79 (0.72, 0.88)	23.8 (20.2, 28.1)	0.288 (0.143, 0.576)	1.51 (1.36, 1.65)
celtsc	<i>Celtis schippii</i>	58.8 (50.2, 69.6)	0.76 (0.69, 0.83)	20.8 (17.2, 25.1)	0.633 (0.277, 1.434)	1.37 (1.14, 1.63)
chr2ar	<i>Chrysophyllum argenteum</i>	57.6 (49.7, 66.3)	0.79 (0.75, 0.84)	27.0 (23.4, 31.3)	0.758 (0.625, 0.924)	1.24 (1.13, 1.35)
chr2ca	<i>Chrysophyllum cainito</i>	63.0 (53.6, 75.8)	0.75 (0.65, 0.85)	22.3 (15.7, 29.3)	0.585 (0.243, 1.405)	1.36 (1.14, 1.58)
phoeci	<i>Cinnamomum triplinerve</i>	55.3 (47.2, 65.4)	0.72 (0.65, 0.81)	19.2 (15.2, 23.6)	0.291 (0.133, 0.659)	1.39 (1.14, 1.64)
conoci	<i>Conostegia cinnamomea</i>	56.9 (48.3, 67.0)	0.71 (0.55, 0.86)	24.7 (20.4, 29.6)	1.380 (0.871, 2.189)	1.15 (0.94, 1.36)
cordal	<i>Cordia alliodora</i>	56.6 (48.7, 66.4)	0.82 (0.74, 0.91)	21.0 (17.0, 25.6)	0.530 (0.221, 1.312)	1.29 (1.05, 1.53)
cordbi	<i>Cordia bicolor</i>	49.9 (42.5, 57.9)	0.86 (0.82, 0.92)	23.9 (20.5, 27.6)	0.270 (0.216, 0.335)	1.44 (1.35, 1.53)
cordla	<i>Cordia lasiocalyx</i>	58.3 (49.4, 69.1)	0.64 (0.57, 0.71)	20.1 (16.4, 24.5)	0.340 (0.200, 0.581)	1.36 (1.16, 1.56)
cou2cu	<i>Coussarea curvigemmia</i>	57.1 (49.1, 66.2)	0.74 (0.68, 0.80)	24.2 (20.3, 28.3)	0.577 (0.360, 0.955)	1.31 (1.12, 1.50)
crotbi	<i>Croton billbergianus</i>	50.0 (42.0, 59.8)	0.77 (0.66, 0.87)	18.9 (14.4, 23.8)	0.732 (0.336, 1.627)	1.34 (1.09, 1.59)
cupala	<i>Cupania latifolia</i>	55.9 (47.3, 66.5)	0.73 (0.63, 0.83)	21.9 (15.9, 27.9)	0.612 (0.267, 1.418)	1.36 (1.13, 1.60)
cupasy	<i>Cupania seemannii</i>	61.4 (51.3, 73.1)	0.65 (0.57, 0.73)	19.4 (15.6, 23.8)	0.800 (0.436, 1.430)	1.36 (1.15, 1.59)
nectpu	<i>Damburneya umbrosa</i>	55.0 (46.7, 64.9)	0.74 (0.68, 0.80)	19.5 (16.1, 23.3)	0.665 (0.319, 1.384)	1.34 (1.09, 1.57)
dendar	<i>Dendropanax arboreus</i>	57.1 (48.6, 68.0)	0.71 (0.62, 0.79)	24.1 (18.6, 30.2)	0.531 (0.243, 1.112)	1.38 (1.18, 1.59)
des2pa	<i>Desmopsis panamensis</i>	60.1 (51.4, 70.6)	0.67 (0.63, 0.71)	22.7 (19.2, 26.9)	0.603 (0.362, 1.016)	1.34 (1.13, 1.54)
dio2ar	<i>Diospyros artanthifolia</i>	58.8 (49.5, 70.0)	0.67 (0.60, 0.74)	17.8 (14.4, 21.8)	0.470 (0.202, 1.043)	1.35 (1.09, 1.61)
diptpa	<i>Dipteryx oleifera</i>	64.5 (57.4, 74.4)	0.80 (0.73, 0.87)	23.0 (19.5, 26.8)	0.530 (0.222, 1.178)	1.47 (1.30, 1.67)
drypst	<i>Drypetes standleyi</i>	55.4 (47.4, 64.3)	0.78 (0.75, 0.82)	22.6 (19.5, 26.2)	0.794 (0.679, 0.933)	1.27 (1.19, 1.34)

Table S2. (continued).

Mnemonic	Species	Tree height (generalized Michaelis-Menten, Eq. 3)			Crown area (power function, Eq. 2)	
		a	b	k	a	b
entesc	Enterolobium schomburgkii	55.5 (46.8, 66.3)	0.77 (0.65, 0.89)	18.9 (13.8, 24.4)	0.880 (0.452, 1.830)	1.23 (0.99, 1.46)
ery2ma	Erythroxylum macrophyllum	60.6 (51.2, 72.1)	0.68 (0.57, 0.79)	23.0 (17.4, 29.3)	0.544 (0.266, 1.202)	1.35 (1.08, 1.61)
eugeco	Eugenia coloradoensis	62.5 (53.4, 74.3)	0.75 (0.69, 0.81)	22.1 (18.4, 26.7)	0.560 (0.273, 1.126)	1.35 (1.12, 1.57)
eugega	Eugenia galalonensis	61.8 (52.7, 73.2)	0.71 (0.64, 0.78)	22.0 (18.0, 26.6)	0.598 (0.341, 1.030)	1.33 (1.14, 1.54)
eugene	Eugenia nesiotica	61.8 (51.9, 73.6)	0.72 (0.63, 0.81)	24.4 (18.9, 30.5)	0.650 (0.277, 1.386)	1.38 (1.15, 1.63)
eugeoe	Eugenia oerstediana	54.8 (46.9, 63.1)	0.77 (0.73, 0.81)	26.9 (23.0, 31.1)	0.803 (0.632, 1.020)	1.34 (1.23, 1.45)
faraoc	Faramea occidentalis	59.1 (50.0, 69.2)	0.65 (0.61, 0.68)	20.5 (17.2, 24.3)	0.663 (0.489, 0.902)	1.25 (1.12, 1.38)
ficuc2	Ficus costaricana	59.6 (50.6, 71.1)	0.70 (0.61, 0.79)	23.4 (17.0, 30.2)	0.564 (0.233, 1.391)	1.18 (0.98, 1.37)
ficuma	Ficus maxima	51.6 (43.7, 61.8)	0.81 (0.69, 0.93)	19.5 (14.5, 25.3)	0.382 (0.183, 0.767)	1.41 (1.17, 1.65)
ficuto	Ficus tonduzii	58.3 (49.3, 69.2)	0.66 (0.56, 0.77)	23.3 (18.0, 29.2)	0.573 (0.260, 1.282)	1.33 (1.07, 1.60)
ficutr	Ficus trigonata	48.5 (41.8, 57.3)	0.81 (0.70, 0.93)	20.4 (15.1, 26.3)	0.651 (0.314, 1.392)	1.30 (1.13, 1.49)
ficuyo	Ficus yoponensis	44.1 (37.5, 53.4)	0.86 (0.74, 1.00)	16.7 (12.2, 22.2)	0.491 (0.249, 0.937)	1.44 (1.27, 1.61)
gar2ma	Garcinia madruno	58.0 (49.4, 68.1)	0.72 (0.67, 0.77)	22.8 (19.3, 26.9)	0.616 (0.275, 1.396)	1.36 (1.09, 1.63)
gar2in	Garcinia recondita	57.6 (49.8, 66.6)	0.77 (0.73, 0.81)	26.7 (22.9, 30.9)	0.819 (0.675, 0.985)	1.26 (1.15, 1.38)
geniam	Genipa americana	63.8 (53.3, 77.4)	0.66 (0.57, 0.76)	24.0 (18.0, 30.5)	0.594 (0.249, 1.327)	1.40 (1.16, 1.65)
guapst	Guapira standleyana	64.4 (55.0, 76.4)	0.70 (0.65, 0.77)	21.9 (18.2, 26.1)	0.597 (0.280, 1.353)	1.29 (1.09, 1.49)
guarsp	Guarea bullata	61.9 (52.5, 73.2)	0.70 (0.63, 0.77)	23.9 (19.8, 28.5)	0.263 (0.141, 0.474)	1.44 (1.25, 1.67)
guargr	Guarea grandifolia	59.3 (50.4, 70.1)	0.74 (0.64, 0.84)	21.8 (15.5, 28.6)	0.601 (0.256, 1.403)	1.34 (1.13, 1.55)
quargu	Guarea guidonia	60.5 (50.5, 73.1)	0.60 (0.53, 0.66)	19.5 (15.5, 23.9)	0.517 (0.239, 1.100)	1.32 (1.10, 1.54)
guatdu	Guatteria lucens	65.0 (55.8, 76.5)	0.74 (0.68, 0.81)	22.0 (18.2, 26.4)	0.635 (0.314, 1.253)	1.29 (1.10, 1.47)
guazul	Guazuma ulmifolia	48.3 (39.7, 58.2)	0.70 (0.62, 0.79)	15.4 (12.0, 19.4)	0.618 (0.275, 1.462)	1.30 (1.08, 1.52)
gustsu	Gustavia superba	54.6 (46.0, 65.2)	0.69 (0.59, 0.78)	21.8 (16.8, 27.4)	0.615 (0.275, 1.364)	1.31 (1.08, 1.52)
tab1gu	Handroanthus guayacan	58.4 (51.1, 67.5)	0.80 (0.74, 0.86)	25.6 (22.4, 29.4)	0.388 (0.210, 0.685)	1.37 (1.23, 1.53)
hassfl	Hasseltia floribunda	60.7 (51.1, 72.1)	0.54 (0.47, 0.62)	20.3 (16.0, 25.2)	0.683 (0.339, 1.410)	1.28 (1.04, 1.50)
heisac	Heisteria acuminata	58.9 (49.9, 69.6)	0.66 (0.61, 0.71)	20.5 (17.0, 24.3)	0.875 (0.439, 1.822)	1.32 (1.04, 1.57)
heisco	Heisteria concinna	48.2 (39.4, 57.5)	0.68 (0.65, 0.72)	15.7 (12.8, 18.8)	0.652 (0.370, 1.153)	1.37 (1.18, 1.55)
hyeral	Hieronyma alchorneoides	64.3 (55.3, 76.2)	0.70 (0.64, 0.77)	23.0 (18.9, 27.4)	0.554 (0.234, 1.337)	1.38 (1.19, 1.58)
hirtam	Hirtella americana	59.3 (49.9, 71.0)	0.62 (0.56, 0.68)	17.6 (14.2, 21.5)	0.485 (0.254, 0.904)	1.42 (1.17, 1.67)
hirttr	Hirtella triandra	57.3 (48.9, 67.2)	0.71 (0.68, 0.74)	23.3 (19.8, 27.3)	0.927 (0.768, 1.130)	1.25 (1.14, 1.36)
ingas1	Inga acuminata	54.6 (45.5, 65.2)	0.67 (0.57, 0.77)	18.7 (13.6, 24.5)	0.735 (0.366, 1.456)	1.40 (1.17, 1.62)
ingago	Inga goldmanii	59.0 (49.8, 70.2)	0.72 (0.62, 0.82)	23.1 (17.1, 29.5)	0.639 (0.271, 1.454)	1.37 (1.13, 1.61)
ingama	Inga marginata	56.1 (47.2, 67.2)	0.69 (0.61, 0.77)	17.5 (13.8, 21.8)	0.658 (0.264, 1.504)	1.40 (1.17, 1.66)
ingasa	Inga sapindoides	58.3 (49.5, 69.3)	0.74 (0.64, 0.83)	22.9 (17.2, 29.0)	0.657 (0.295, 1.463)	1.38 (1.13, 1.63)
ingasp	Inga spectabilis	53.5 (45.3, 63.6)	0.73 (0.62, 0.83)	22.1 (16.3, 28.3)	0.541 (0.233, 1.231)	1.37 (1.12, 1.61)
ingaum	Inga umbellifera	63.5 (53.0, 76.4)	0.59 (0.51, 0.66)	17.2 (14.0, 21.2)	0.881 (0.408, 1.959)	1.32 (1.05, 1.57)
jac1co	Jacaranda copaia	51.4 (45.1, 60.0)	0.75 (0.68, 0.83)	14.6 (12.3, 17.1)	0.500 (0.269, 0.977)	1.36 (1.20, 1.52)
laciag	Lacistema aggregatum	62.0 (52.5, 73.8)	0.71 (0.66, 0.77)	21.9 (18.3, 26.4)	0.467 (0.198, 1.074)	1.35 (1.09, 1.63)
lacmpa	Lacistema panamensis	53.4 (44.9, 63.6)	0.69 (0.62, 0.77)	17.4 (14.0, 21.3)	0.538 (0.245, 1.371)	1.31 (1.06, 1.55)
laetpr	Laetia procera	48.2 (40.6, 57.8)	0.81 (0.71, 0.93)	17.2 (13.2, 21.8)	0.591 (0.253, 1.422)	1.40 (1.16, 1.63)
laeth	Laetia thamnia	60.3 (50.8, 72.1)	0.65 (0.59, 0.70)	18.0 (14.8, 21.7)	0.705 (0.311, 1.577)	1.38 (1.10, 1.65)
licahy	Licania hypoleuca	62.5 (52.6, 74.2)	0.67 (0.63, 0.71)	20.7 (17.2, 24.8)	0.725 (0.323, 1.560)	1.36 (1.11, 1.61)
licapl	Licania platypus	61.0 (51.7, 72.8)	0.72 (0.63, 0.82)	23.4 (17.5, 29.7)	0.639 (0.310, 1.432)	1.24 (1.00, 1.44)
lindla	Lindackeria laurina	57.4 (48.2, 68.6)	0.71 (0.60, 0.80)	23.3 (17.5, 29.3)	0.488 (0.219, 1.090)	1.35 (1.10, 1.59)
loncla	Lonchocarpus heptaphyllus	63.9 (54.5, 75.5)	0.75 (0.70, 0.81)	21.4 (17.8, 25.7)	0.189 (0.112, 0.320)	1.53 (1.38, 1.70)
luehse	Luehea seemannii	55.1 (48.7, 62.9)	0.78 (0.74, 0.83)	26.9 (23.6, 30.5)	0.526 (0.230, 1.262)	1.33 (1.13, 1.52)
macrgl	Macrocnemum roseum	59.4 (50.2, 70.6)	0.71 (0.61, 0.81)	23.7 (17.6, 30.0)	0.569 (0.247, 1.312)	1.30 (1.06, 1.54)

Table S2. (continued).

Mnemonic	Species	Tree height (generalized Michaelis-Menten, Eq. 3)			Crown area (power function, Eq. 2)	
		a	b	k	a	b
maquco	<i>Maquira guianensis</i>	59.1 (50.2, 69.5)	0.68 (0.63, 0.74)	21.2 (17.6, 25.4)	0.517 (0.297, 0.902)	1.33 (1.12, 1.53)
mar1la	<i>Marila laxiflora</i>	56.2 (48.0, 65.9)	0.64 (0.51, 0.77)	23.0 (19.1, 27.6)	0.647 (0.406, 1.032)	1.33 (1.13, 1.52)
maytsc	<i>Maytenus schippii</i>	61.4 (51.8, 73.6)	0.75 (0.64, 0.85)	21.7 (15.5, 28.0)	0.525 (0.226, 1.230)	1.34 (1.07, 1.61)
micoar	<i>Miconia argentea</i>	50.8 (42.7, 60.1)	0.79 (0.74, 0.85)	18.2 (15.3, 21.7)	0.626 (0.480, 0.814)	1.34 (1.22, 1.46)
micone	<i>Miconia nervosa</i>	54.9 (46.3, 64.2)	0.70 (0.56, 0.84)	24.3 (19.9, 29.2)	0.862 (0.556, 1.301)	1.26 (1.06, 1.46)
malmsp	<i>Mosannona garwoodii</i>	60.1 (50.8, 70.9)	0.70 (0.65, 0.76)	20.4 (16.9, 24.3)	0.468 (0.212, 1.030)	1.37 (1.11, 1.62)
mourmy	<i>Mouriri myrtilloides</i>	62.5 (52.7, 74.2)	0.51 (0.46, 0.57)	19.4 (16.2, 23.4)	0.898 (0.579, 1.406)	1.32 (1.12, 1.53)
myrcga	<i>Myrcia splendens</i> tip. <i>gatunensis</i>	61.2 (51.5, 73.5)	0.64 (0.56, 0.72)	17.8 (14.3, 21.8)	0.642 (0.325, 1.301)	1.34 (1.08, 1.58)
myrofr	<i>Myrospermum frutescens</i>	66.4 (55.8, 79.6)	0.76 (0.65, 0.86)	20.7 (14.6, 27.4)	0.423 (0.180, 0.923)	1.47 (1.24, 1.73)
nectci	<i>Nectandra cissiflora</i>	55.6 (46.3, 66.4)	0.75 (0.62, 0.87)	17.2 (11.6, 23.6)	0.518 (0.238, 1.146)	1.35 (1.10, 1.61)
ochrpy	<i>Ochroma pyramidale</i>	34.6 (28.1, 44.7)	0.90 (0.73, 1.08)	13.4 (6.4, 21.0)	0.702 (0.260, 1.815)	1.39 (1.14, 1.64)
ocotob	<i>Ocotea oblonga</i>	51.4 (43.2, 61.2)	0.75 (0.64, 0.85)	20.5 (14.7, 26.5)	0.562 (0.239, 1.312)	1.31 (1.07, 1.54)
ocotpu	<i>Ocotea puberula</i>	56.5 (47.9, 67.1)	0.75 (0.65, 0.86)	20.9 (14.6, 27.9)	0.584 (0.232, 1.364)	1.37 (1.14, 1.60)
ocotwh	<i>Ocotea whitei</i>	57.4 (49.3, 67.6)	0.78 (0.69, 0.88)	22.0 (16.9, 27.5)	0.717 (0.339, 1.584)	1.24 (1.04, 1.43)
ormocr	<i>Ormosia coccinea</i>	60.0 (51.0, 71.6)	0.77 (0.66, 0.88)	21.3 (15.9, 27.0)	0.391 (0.192, 0.850)	1.33 (1.13, 1.55)
ormoma	<i>Ormosia macrocalyx</i>	58.2 (50.1, 68.2)	0.81 (0.73, 0.91)	28.1 (23.2, 33.5)	0.264 (0.150, 0.467)	1.43 (1.26, 1.61)
ouralu	<i>Ouratea lucens</i>	66.2 (55.9, 79.0)	0.74 (0.67, 0.82)	21.2 (17.6, 25.6)	0.288 (0.147, 0.527)	1.47 (1.24, 1.72)
pochse	<i>Pachira sessilis</i>	58.1 (50.2, 68.3)	0.78 (0.72, 0.84)	20.4 (17.2, 24.4)	0.504 (0.299, 0.861)	1.25 (1.07, 1.41)
perexa	<i>Perebea xanthochyma</i>	59.7 (50.6, 70.9)	0.66 (0.62, 0.71)	19.7 (16.5, 23.4)	0.666 (0.306, 1.493)	1.33 (1.06, 1.58)
picrla	<i>Picramnia latifolia</i>	63.4 (53.2, 76.2)	0.56 (0.48, 0.64)	19.7 (15.7, 24.3)	0.147 (0.070, 0.281)	1.77 (1.54, 2.04)
pipere	<i>Piper reticulatum</i>	56.7 (48.3, 67.3)	0.72 (0.60, 0.84)	22.1 (17.0, 27.8)	0.660 (0.338, 1.342)	1.32 (1.04, 1.56)
pla1pi	<i>Platymiscium pinnatum</i>	65.7 (56.1, 78.3)	0.68 (0.60, 0.75)	18.7 (14.7, 23.3)	0.479 (0.199, 1.174)	1.35 (1.12, 1.56)
pla2el	<i>Platypodium elegans</i>	59.3 (52.0, 68.8)	0.77 (0.70, 0.85)	23.3 (19.9, 27.3)	0.811 (0.353, 1.804)	1.22 (1.04, 1.41)
hybapr	<i>Pombalia prunifolia</i>	61.8 (52.3, 72.8)	0.51 (0.45, 0.58)	22.6 (19.0, 27.0)	0.834 (0.508, 1.365)	1.26 (1.05, 1.47)
poular	<i>Poulsonia armata</i>	57.4 (51.4, 64.8)	0.86 (0.82, 0.91)	33.1 (29.4, 37.4)	0.332 (0.168, 0.636)	1.32 (1.16, 1.50)
pourbi	<i>Pouroma bicolor</i>	51.1 (42.4, 61.2)	0.71 (0.64, 0.78)	16.4 (13.4, 19.8)	0.600 (0.237, 1.520)	1.39 (1.14, 1.65)
poutre	<i>Pouteria reticulata</i>	63.3 (54.5, 75.0)	0.71 (0.66, 0.75)	20.6 (17.5, 24.5)	0.690 (0.400, 1.225)	1.32 (1.16, 1.47)
pri2co	<i>Prioria copaifera</i>	60.1 (55.4, 65.7)	0.86 (0.83, 0.89)	36.5 (33.9, 39.5)	0.908 (0.787, 1.050)	1.18 (1.14, 1.22)
protsp	<i>Protium confusum</i>	54.5 (45.5, 64.7)	0.68 (0.62, 0.75)	16.7 (13.7, 20.2)	0.760 (0.482, 1.179)	1.25 (1.05, 1.44)
protco	<i>Protium costaricense</i>	60.8 (51.0, 72.9)	0.61 (0.54, 0.69)	19.3 (15.2, 23.9)	0.661 (0.328, 1.308)	1.38 (1.14, 1.61)
protpa	<i>Protium panamense</i>	61.8 (52.2, 73.8)	0.68 (0.65, 0.72)	19.8 (16.7, 23.7)	0.356 (0.201, 0.636)	1.42 (1.22, 1.62)
protte	<i>Protium tenuifolium</i> subsp. <i>sessiliflorum</i>	50.1 (40.8, 59.7)	0.75 (0.71, 0.81)	21.2 (17.5, 25.2)	0.565 (0.436, 0.743)	1.37 (1.26, 1.47)
pse1se	<i>Pseudobombax septenatum</i>	52.7 (45.6, 62.2)	0.80 (0.70, 0.90)	20.6 (14.6, 26.9)	0.550 (0.240, 1.351)	1.28 (1.06, 1.48)
psycma	<i>Psychotria marginata</i>	56.9 (48.5, 66.6)	0.68 (0.55, 0.81)	26.1 (21.5, 31.0)	0.552 (0.347, 0.868)	1.36 (1.17, 1.56)
ptero	<i>Pterocarpus hayesii</i>	62.8 (53.9, 73.8)	0.75 (0.69, 0.81)	23.3 (19.8, 27.6)	0.534 (0.289, 1.044)	1.37 (1.17, 1.55)
quaras	<i>Quararibea asterolepis</i>	57.8 (52.1, 64.6)	0.86 (0.82, 0.89)	32.0 (29.1, 35.5)	1.052 (0.884, 1.253)	1.09 (1.03, 1.14)
quasam	<i>Quassia amara</i>	63.9 (53.9, 76.2)	0.56 (0.50, 0.62)	21.5 (17.8, 26.0)	0.591 (0.280, 1.264)	1.34 (1.07, 1.60)
randar	<i>Randia armata</i>	61.3 (51.8, 72.9)	0.52 (0.45, 0.60)	20.6 (16.3, 25.4)	0.771 (0.351, 1.651)	1.35 (1.11, 1.59)
rinosy	<i>Rinorea sylvatica</i>	61.2 (52.3, 71.6)	0.64 (0.59, 0.69)	24.9 (21.1, 29.4)	1.095 (0.593, 2.023)	1.27 (1.03, 1.50)
sapiau	<i>Sapium glandulosum</i>	57.1 (49.2, 67.2)	0.80 (0.71, 0.90)	22.2 (16.6, 28.3)	0.489 (0.206, 1.084)	1.40 (1.19, 1.63)
simaam	<i>Simarouba amara</i>	39.9 (35.8, 44.8)	1.01 (0.97, 1.06)	21.9 (19.7, 24.6)	0.538 (0.458, 0.631)	1.32 (1.25, 1.40)
sipacr	<i>Siparuna cristata</i>	58.6 (49.3, 69.6)	0.76 (0.64, 0.89)	21.7 (16.7, 27.3)	0.680 (0.358, 1.274)	1.30 (1.06, 1.55)
sloate	<i>Sloanea terniflora</i>	55.7 (49.4, 62.8)	0.92 (0.87, 0.97)	33.0 (29.4, 37.0)	0.546 (0.429, 0.690)	1.35 (1.27, 1.43)
soroaf	<i>Sorocea affinis</i>	61.6 (52.1, 72.8)	0.61 (0.57, 0.65)	21.5 (17.9, 25.6)	0.356 (0.210, 0.611)	1.37 (1.16, 1.58)
sponmo	<i>Spondias mombin</i>	50.1 (42.4, 59.7)	0.78 (0.68, 0.89)	20.0 (14.2, 26.3)	0.526 (0.223, 1.248)	1.42 (1.21, 1.63)
sponra	<i>Spondias radlkoferi</i>	54.2 (47.1, 62.2)	0.80 (0.76, 0.85)	28.3 (24.5, 32.3)	0.238 (0.179, 0.314)	1.54 (1.44, 1.65)
sterap	<i>Sterculia apetala</i>	59.3 (52.3, 67.5)	0.82 (0.76, 0.89)	26.9 (23.2, 31.2)	0.487 (0.247, 0.966)	1.39 (1.23, 1.57)

Table S2. (continued).

Mnemonic	Species	Tree height (generalized Michaelis-Menten, Eq. 3)			Crown area (power function, Eq. 2)	
		a	b	k	a	b
swars2	<i>Swartzia simplex</i> var. <i>continentalis</i>	64.6 (54.4, 76.7)	0.60 (0.56, 0.64)	22.1 (18.5, 26.5)	0.378 (0.216, 0.637)	1.55 (1.37, 1.75)
swars1	<i>Swartzia simplex</i> var. <i>grandiflora</i>	64.9 (54.6, 78.0)	0.56 (0.50, 0.62)	18.6 (15.0, 23.0)	0.482 (0.254, 0.870)	1.48 (1.30, 1.69)
sympgl	<i>Sympmania globulifera</i>	58.6 (49.8, 69.9)	0.78 (0.67, 0.88)	20.5 (14.1, 27.0)	0.546 (0.227, 1.295)	1.36 (1.13, 1.61)
tab1ro	<i>Tabebuia rosea</i>	58.9 (52.3, 66.5)	0.92 (0.86, 0.98)	28.8 (25.5, 32.6)	0.384 (0.289, 0.506)	1.42 (1.33, 1.51)
tab2ar	<i>Tabernaemontana arborea</i>	62.0 (53.5, 73.3)	0.66 (0.61, 0.71)	23.4 (19.5, 27.8)	0.552 (0.298, 1.013)	1.29 (1.13, 1.45)
tachve	<i>Tachigali panamensis</i>	49.7 (44.1, 55.8)	0.97 (0.92, 1.03)	28.9 (26.0, 32.2)	0.647 (0.540, 0.778)	1.43 (1.36, 1.49)
talipr	<i>Talisia croatii</i>	63.0 (53.1, 75.3)	0.73 (0.61, 0.85)	23.8 (18.1, 30.1)	0.131 (0.064, 0.260)	1.48 (1.23, 1.75)
taline	<i>Talisia nervosa</i>	65.2 (54.7, 77.4)	0.60 (0.55, 0.66)	23.5 (19.4, 28.1)	0.216 (0.103, 0.436)	1.48 (1.23, 1.75)
termam	<i>Terminalia amazonia</i>	58.7 (50.5, 69.3)	0.77 (0.66, 0.88)	19.4 (13.7, 25.8)	0.556 (0.232, 1.316)	1.44 (1.21, 1.66)
termob	<i>Terminalia oblonga</i>	59.9 (52.2, 69.7)	0.85 (0.77, 0.93)	25.0 (20.6, 30.0)	0.624 (0.281, 1.390)	1.43 (1.23, 1.63)
tet2pa	<i>Tetragastris panamensis</i>	57.0 (50.0, 65.2)	0.72 (0.70, 0.75)	19.9 (17.5, 22.8)	0.467 (0.397, 0.556)	1.46 (1.40, 1.52)
tocopi	<i>Tocoyena pittieri</i>	53.3 (45.0, 63.7)	0.73 (0.63, 0.83)	22.4 (17.2, 28.1)	0.678 (0.339, 1.314)	1.32 (1.12, 1.53)
tratas	<i>Trattinnickia aspera</i>	50.4 (42.7, 60.5)	0.74 (0.64, 0.84)	14.9 (11.7, 18.6)	0.537 (0.221, 1.255)	1.36 (1.13, 1.58)
tremmi	<i>Trema micrantha</i>	38.6 (31.0, 49.0)	0.88 (0.72, 1.04)	15.0 (8.4, 22.4)	0.605 (0.241, 1.403)	1.42 (1.20, 1.66)
tri2pa	<i>Trichilia pallida</i>	57.1 (48.3, 68.0)	0.68 (0.58, 0.78)	23.3 (17.5, 29.3)	0.598 (0.266, 1.327)	1.35 (1.10, 1.60)
tri2tu	<i>Trichilia tuberculata</i>	57.9 (51.0, 65.7)	0.83 (0.80, 0.85)	27.7 (24.4, 31.5)	0.847 (0.728, 0.988)	1.19 (1.13, 1.24)
tripcu	<i>Triplaris cumingiana</i>	59.0 (50.4, 70.4)	0.79 (0.68, 0.90)	19.8 (13.4, 26.4)	0.474 (0.204, 1.150)	1.27 (1.01, 1.50)
tur poc	<i>Turpinia occidentalis</i>	48.5 (40.3, 57.8)	0.72 (0.62, 0.81)	22.5 (17.0, 28.5)	0.561 (0.232, 1.448)	1.20 (0.94, 1.43)
unonpi	<i>Unonopsis pittieri</i>	58.5 (49.5, 69.7)	0.76 (0.66, 0.87)	21.3 (15.4, 27.7)	0.428 (0.194, 1.007)	1.30 (1.03, 1.55)
virosp	<i>Virola multiflora</i>	55.3 (47.4, 64.7)	0.78 (0.72, 0.84)	20.2 (17.1, 23.8)	0.489 (0.217, 1.306)	1.31 (1.06, 1.53)
virosu	<i>Virola nobilis</i>	65.0 (57.2, 75.4)	0.76 (0.71, 0.81)	24.1 (20.9, 27.8)	0.477 (0.231, 1.056)	1.35 (1.15, 1.52)
virose	<i>Virola sebifera</i>	57.9 (49.7, 67.4)	0.79 (0.75, 0.84)	24.4 (21.0, 28.2)	0.871 (0.499, 1.553)	1.19 (1.01, 1.36)
vochfe	<i>Vochysia ferruginea</i>	50.0 (41.8, 59.8)	0.78 (0.66, 0.90)	18.4 (13.1, 24.4)	0.470 (0.210, 1.030)	1.42 (1.18, 1.67)
xyl1ma	<i>Xylopia macrantha</i>	54.0 (46.0, 63.9)	0.76 (0.72, 0.79)	19.1 (16.1, 22.6)	0.992 (0.537, 1.908)	1.24 (1.02, 1.45)
zantbe	<i>Zanthoxylum ekmanii</i>	44.1 (38.3, 52.4)	0.89 (0.77, 1.01)	16.8 (13.1, 21.0)	0.442 (0.200, 0.950)	1.41 (1.21, 1.62)
zantp1	<i>Zanthoxylum panamense</i>	60.1 (50.9, 71.5)	0.77 (0.67, 0.88)	20.1 (14.1, 26.7)	0.496 (0.206, 1.111)	1.43 (1.21, 1.67)

Table S3. Posterior estimates of the parameters of the hierarchical models for tree height allometry. Table entries correspond to the mean and 90% posterior central intervals for the community level parameters of each allometric function (see Eq. 5 in Methods).

Posterior parameter estimates for tree height models

Functional form		Covariate	α (Mean)	β (Slope)	σ (Variation)
gMM	Growth	a	57.05 (54.48, 59.97)	-0.09332 (-0.133, -0.04791)	0.1075 (0.08175, 0.1373)
		b	0.7348 (0.7176, 0.7524)	0.0374 (0.01427, 0.06038)	0.09253 (0.08194, 0.105)
		k	21.77 (20.7, 22.89)	-1.801 (-2.812, -0.7942)	4.176 (3.637, 4.801)
gMM	Wood density	a	57.08 (54.65, 59.91)	0.03953 (-0.002625, 0.08066)	0.09861 (0.07084, 0.1275)
		b	0.7321 (0.7153, 0.7487)	-0.02491 (-0.04179, -0.007441)	0.09084 (0.08043, 0.1031)
		k	21.75 (20.74, 22.86)	-0.1737 (-1.14, 0.8306)	4.123 (3.604, 4.746)
gMM	Mortality	a	57.24 (54.65, 60.29)	-0.0717 (-0.1192, -0.02381)	0.09581 (0.06977, 0.1238)
		b	0.7323 (0.715, 0.7495)	0.02643 (0.007359, 0.04402)	0.09153 (0.08104, 0.1033)
		k	21.81 (20.7, 23.01)	-0.9538 (-2.126, 0.1576)	4.14 (3.631, 4.74)
gMM	None	a	57.17 (54.69, 59.87)		0.1012 (0.07492, 0.1295)
		b	0.7278 (0.7113, 0.7456)		0.0929 (0.08251, 0.1057)
		k	21.57 (20.54, 22.66)		4.194 (3.666, 4.822)
Power	Growth	a	3.029 (2.936, 3.125)	0.05567 (0.03785, 0.07331)	0.1021 (0.0905, 0.1154)
		b	0.5576 (0.5465, 0.5687)	-0.03353 (-0.04574, -0.02132)	0.06988 (0.06218, 0.07942)
Power	Wood density	a	2.988 (2.896, 3.082)	-0.0006186 (-0.01776, 0.01625)	0.1117 (0.09968, 0.1257)
		b	0.5609 (0.5501, 0.5723)	0.01287 (0.001632, 0.02434)	0.0707 (0.06283, 0.07958)
Power	Mortality	a	2.994 (2.902, 3.091)	0.01294 (-0.004155, 0.03049)	0.1116 (0.09976, 0.1254)
		b	0.5604 (0.5489, 0.5714)	-0.01608 (-0.02736, -0.004805)	0.07063 (0.06258, 0.08001)
Power	None	a	2.979 (2.888, 3.076)		0.1113 (0.09941, 0.1253)
		b	0.5616 (0.5501, 0.573)		0.07094 (0.06295, 0.08077)
Weibull	Growth	a	40.99 (39.52, 42.56)	-2.06 (-3.15, -0.7914)	4.089 (3.202, 5.097)
		b	0.0675 (0.06473, 0.07056)	0.004051 (0.001157, 0.006867)	0.01169 (0.009993, 0.01369)
		k	0.6995 (0.6844, 0.7145)	0.02407 (0.00513, 0.04369)	0.08835 (0.07873, 0.09955)
Weibull	Wood density	a	40.98 (39.53, 42.52)	0.5059 (-0.7509, 1.743)	3.981 (3.094, 5.009)
		b	0.06717 (0.06442, 0.07025)	0.001369 (-0.001021, 0.003836)	0.01157 (0.009918, 0.01366)
		k	0.6976 (0.6835, 0.7125)	-0.01604 (-0.03077, -0.001495)	0.0871 (0.07755, 0.09825)
Weibull	Mortality	a	41.09 (39.57, 42.68)	-1.287 (-2.798, 0.1783)	3.886 (3.022, 4.896)
		b	0.06712 (0.06412, 0.07019)	0.0008289 (-0.001922, 0.003454)	0.01155 (0.009865, 0.0135)
		k	0.6978 (0.6829, 0.7129)	0.01537 (-0.0008984, 0.03091)	0.08763 (0.07749, 0.09876)
Weibull	None	a	40.99 (39.53, 42.59)		4.081 (3.148, 5.095)
		b	0.06767 (0.06469, 0.07072)		0.01191 (0.01016, 0.01385)
		k	0.6954 (0.6809, 0.7106)		0.08858 (0.07873, 0.1004)

Table S4. Posterior estimates of the parameters of the hierarchical models for crown area allometry. Table entries correspond to the mean and 90% posterior central intervals for the community level parameters of each allometric function (see Eq. 5 in Methods).

Posterior parameter estimates for crown area models

Functional form	Covariate	α (Mean)	β (Slope)	σ (Variation)
gMM	Growth	a 418 (363.4, 473.2)	0.08395 (-0.03009, 0.1973)	0.3042 (0.2406, 0.3647)
		b 1.427 (1.395, 1.461)	0.02819 (-0.007316, 0.06313)	0.09068 (0.07131, 0.1141)
		k 780.3 (694.9, 868.7)	93.05 (11.69, 170.7)	160.6 (33.13, 226.8)
gMM	Wood density	a 423.8 (366.1, 485.5)	-0.02087 (-0.1385, 0.09542)	0.3172 (0.2575, 0.3783)
		b 1.424 (1.391, 1.459)	-0.004723 (-0.03743, 0.03022)	0.0978 (0.07692, 0.1208)
		k 775.9 (690.5, 869.8)	-48.16 (-124.3, 25.78)	141 (41.78, 227.7)
gMM	Mortality	a 411.5 (362, 471.1)	0.05977 (-0.05878, 0.1709)	0.3052 (0.252, 0.3663)
		b 1.428 (1.397, 1.46)	0.03795 (0.005023, 0.06967)	0.09006 (0.0716, 0.1121)
		k 771.8 (688.1, 864.7)	70.19 (3.028, 133.6)	158.4 (87.77, 221.3)
gMM	None	a 423.3 (373.3, 484.4)		0.3114 (0.2512, 0.3757)
		b 1.421 (1.39, 1.456)		0.09434 (0.07534, 0.1175)
		k 768.3 (699.7, 864.6)		164.1 (71.55, 239.1)
<hr/>				
Power	Growth	a 0.568 (0.5075, 0.6384)	0.02852 (-0.02939, 0.08544)	0.3065 (0.2644, 0.3537)
		b 1.34 (1.303, 1.374)	0.005619 (-0.03522, 0.04613)	0.1511 (0.1176, 0.1916)
Power	Wood density	a 0.5571 (0.4981, 0.6282)	0.05064 (-0.001368, 0.1046)	0.3033 (0.2598, 0.3533)
		b 1.346 (1.309, 1.38)	0.01092 (-0.02278, 0.04919)	0.1534 (0.1213, 0.1927)
Power	Mortality	a 0.5689 (0.5029, 0.6385)	0.02877 (-0.02567, 0.07852)	0.3096 (0.2662, 0.3556)
		b 1.339 (1.305, 1.375)	0.001199 (-0.03549, 0.03631)	0.1538 (0.1209, 0.1942)
Power	None	a 0.5659 (0.5032, 0.6346)		0.3033 (0.2593, 0.3518)
		b 1.341 (1.306, 1.376)		0.1558 (0.1241, 0.1953)
<hr/>				
Weibull	Growth	a 469.1 (408.2, 540)	50.35 (-7.432, 103.7)	114 (73.99, 149.8)
		b 0.0012 (0.001036, 0.001413)	-0.0001886 (-0.0003151, -7.218e-05)	0.0002285 (0.0001421, 0.0003643)
		k 1.397 (1.372, 1.43)	0.0385 (0.008854, 0.0715)	0.0859 (0.06889, 0.1032)
Weibull	Wood density	a 477.1 (406.8, 558.8)	-46.71 (-99.32, 10.12)	124.9 (82.05, 154.6)
		b 0.001211 (0.001036, 0.001415)	0.0002207 (3.596e-05, 0.0003439)	0.0001932 (0.0001311, 0.0003464)
		k 1.395 (1.365, 1.42)	-0.003965 (-0.0363, 0.02225)	0.08728 (0.07315, 0.1057)
Weibull	Mortality	a 466.9 (408, 531.5)	57.68 (12.43, 93.66)	114.3 (87.85, 144.1)
		b 0.001226 (0.001064, 0.001418)	-0.0002813 (-0.0003917, -0.0001416)	0.0002179 (0.0001356, 0.0003161)
		k 1.397 (1.371, 1.424)	0.04507 (0.01622, 0.07342)	0.08366 (0.06676, 0.103)
Weibull	None	a 486.7 (422.1, 559.4)		115.6 (52.38, 158.1)
		b 0.001174 (0.001009, 0.001351)		0.0002555 (6.624e-05, 0.0003783)
		k 1.389 (1.364, 1.416)		0.08765 (0.07073, 0.1066)

Figure S1. Species-specific relationships of tree height with trunk diameter, showing the data (points) and fitted relationships (solid lines) together with their 90% posterior central intervals (dashed lines). The annotations on each plot detail sample size (n) and the observed range of tree heights (H) for each species. Note the log–log axes (multiple pages).

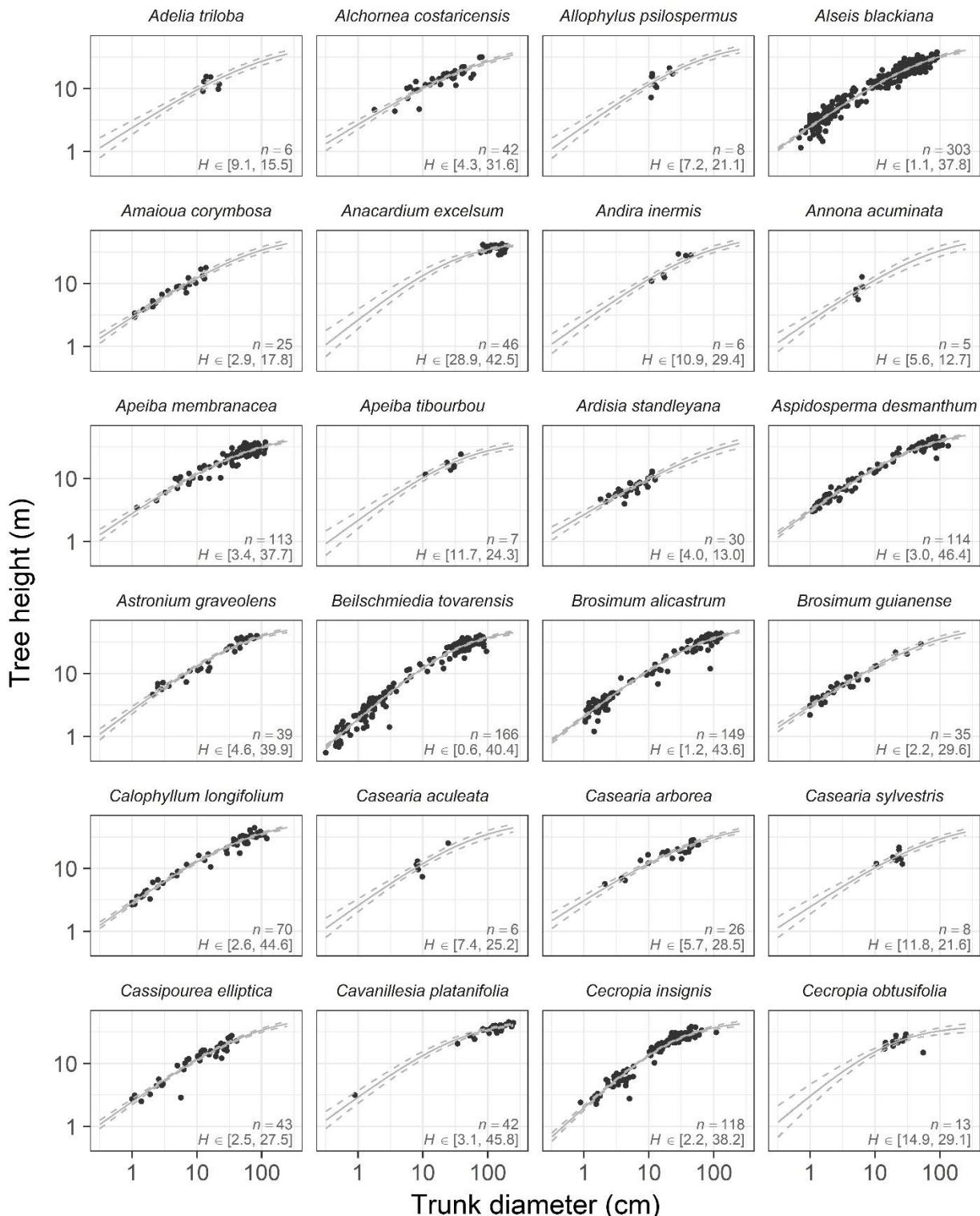


Figure S1. (continued).

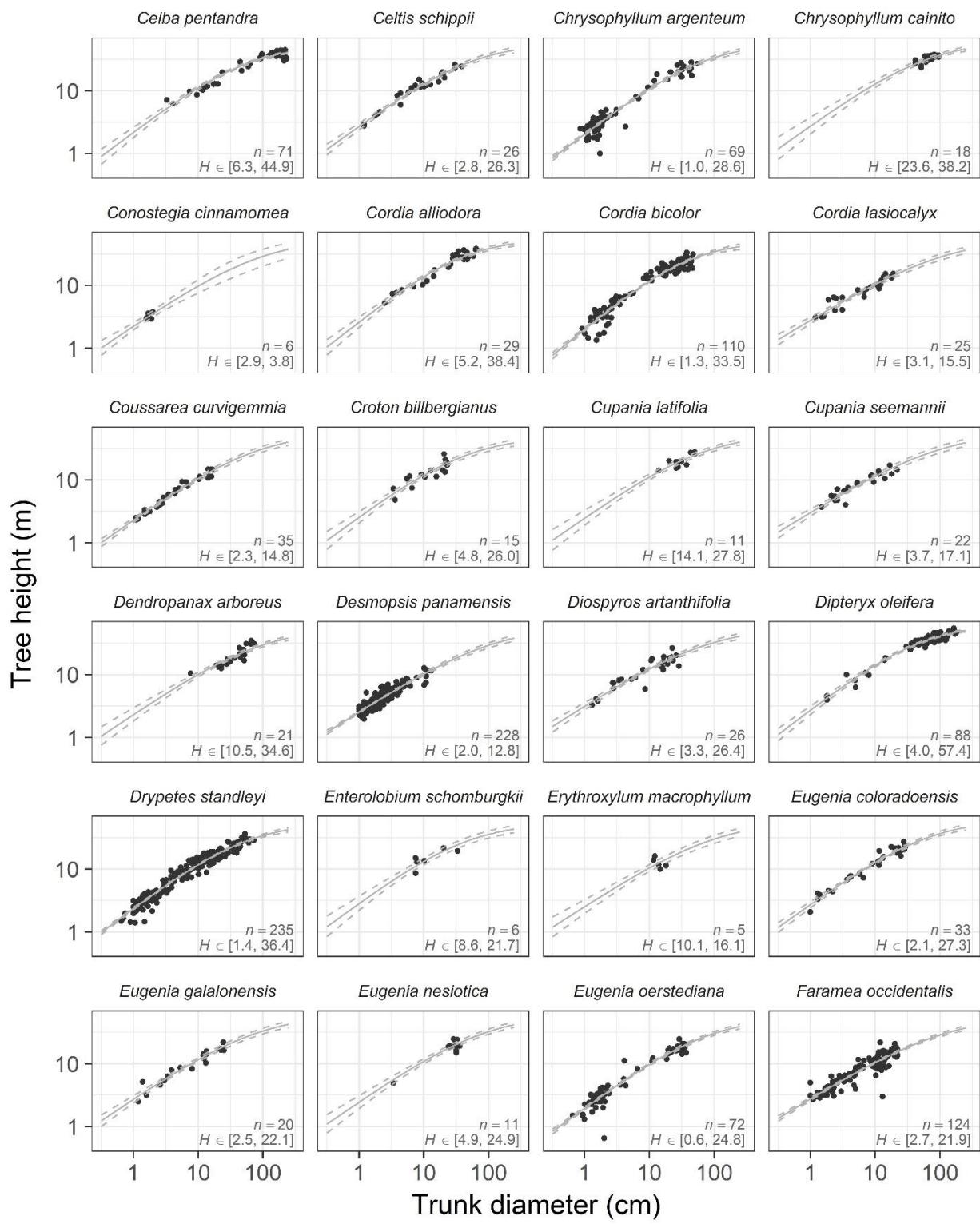


Figure S1. (continued).

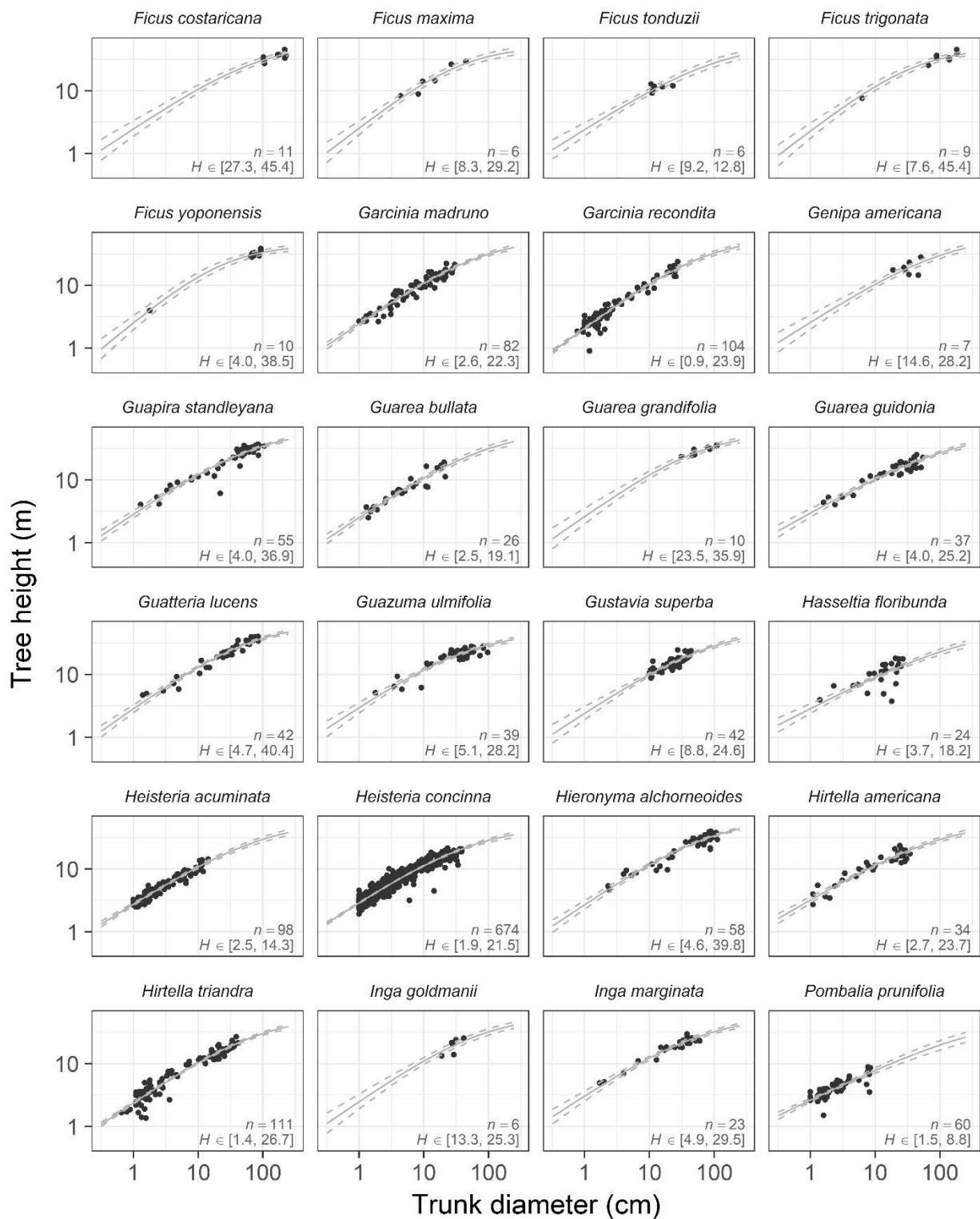


Figure S1. (continued).

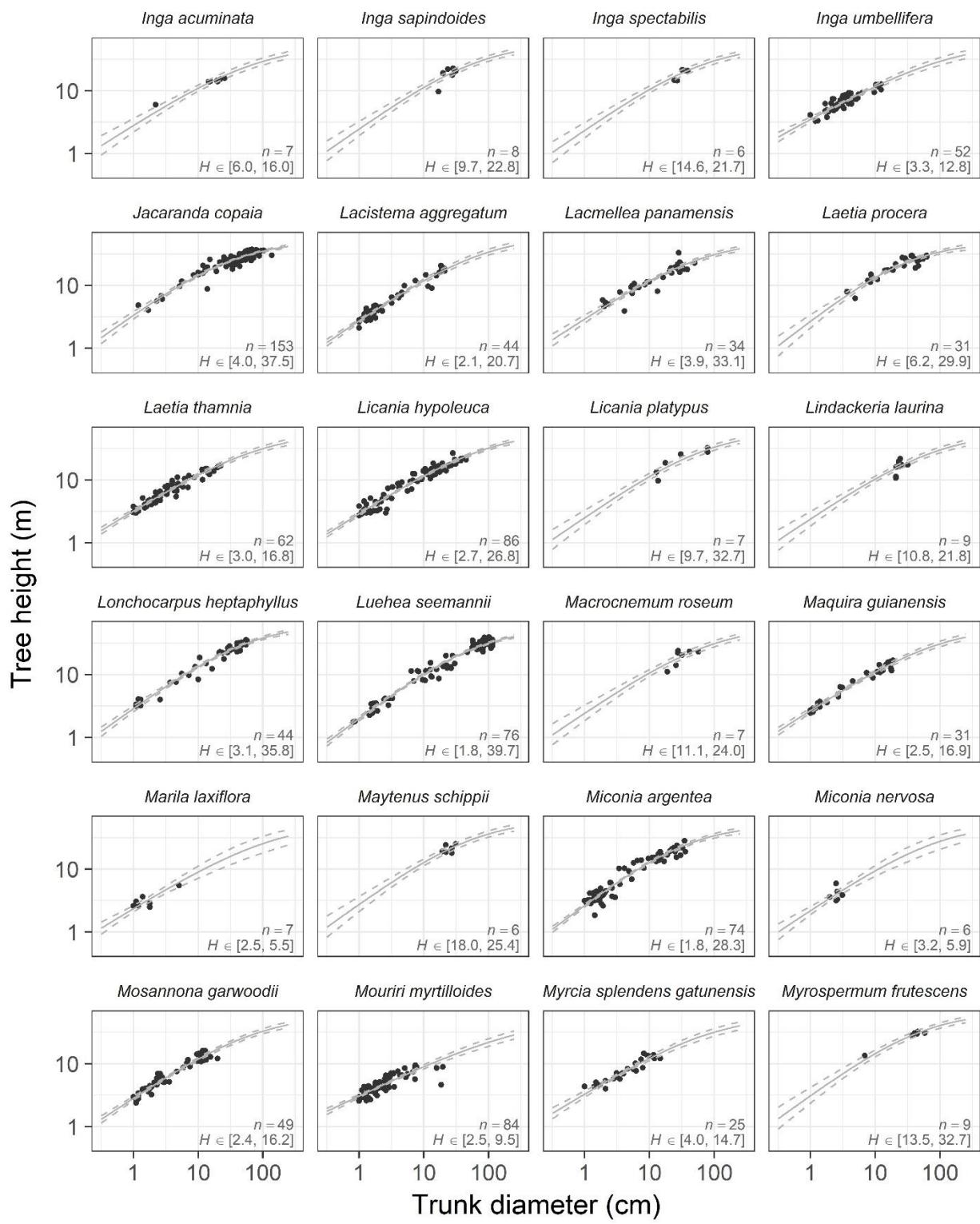


Figure S1. (continued).

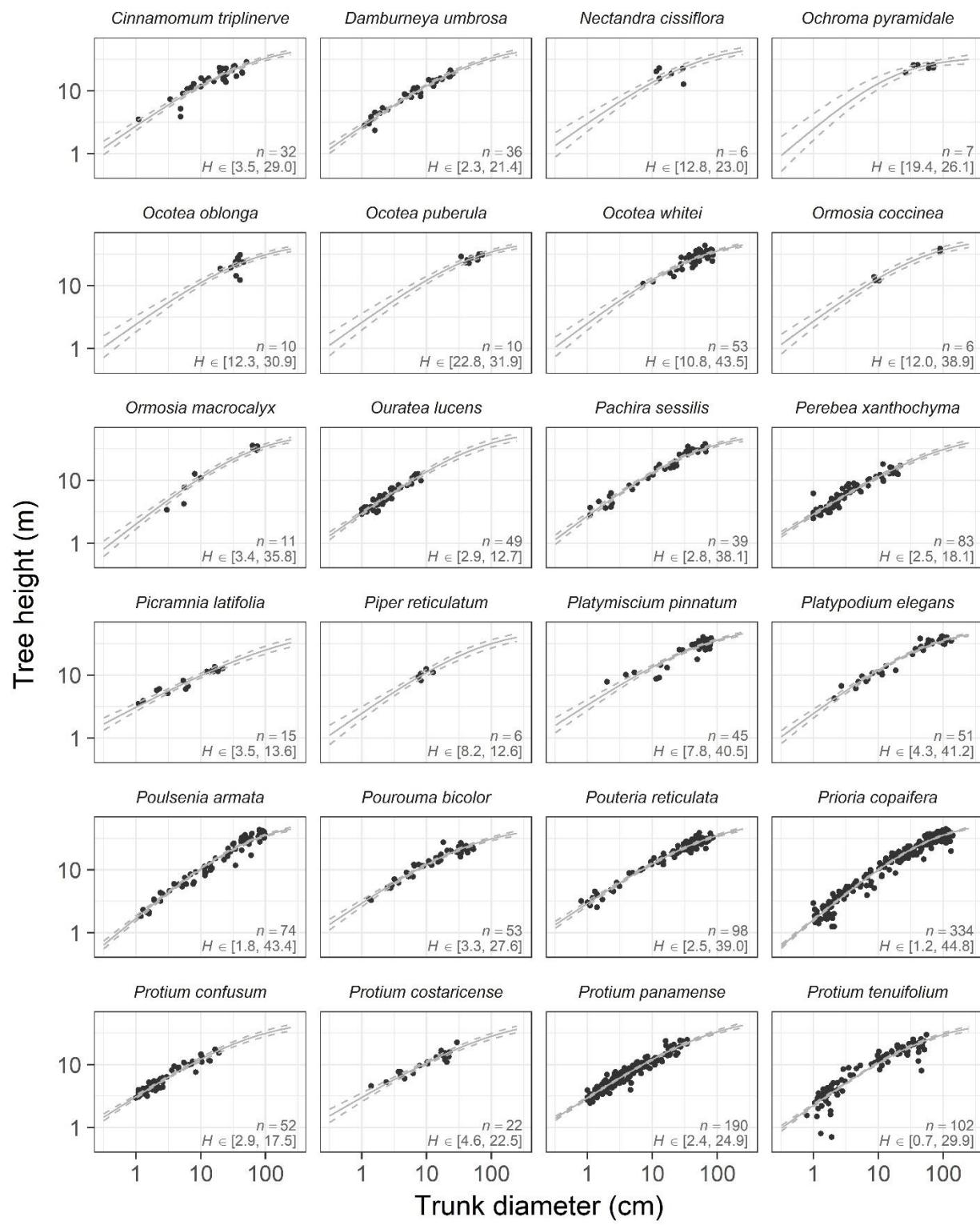


Figure S1. (continued).

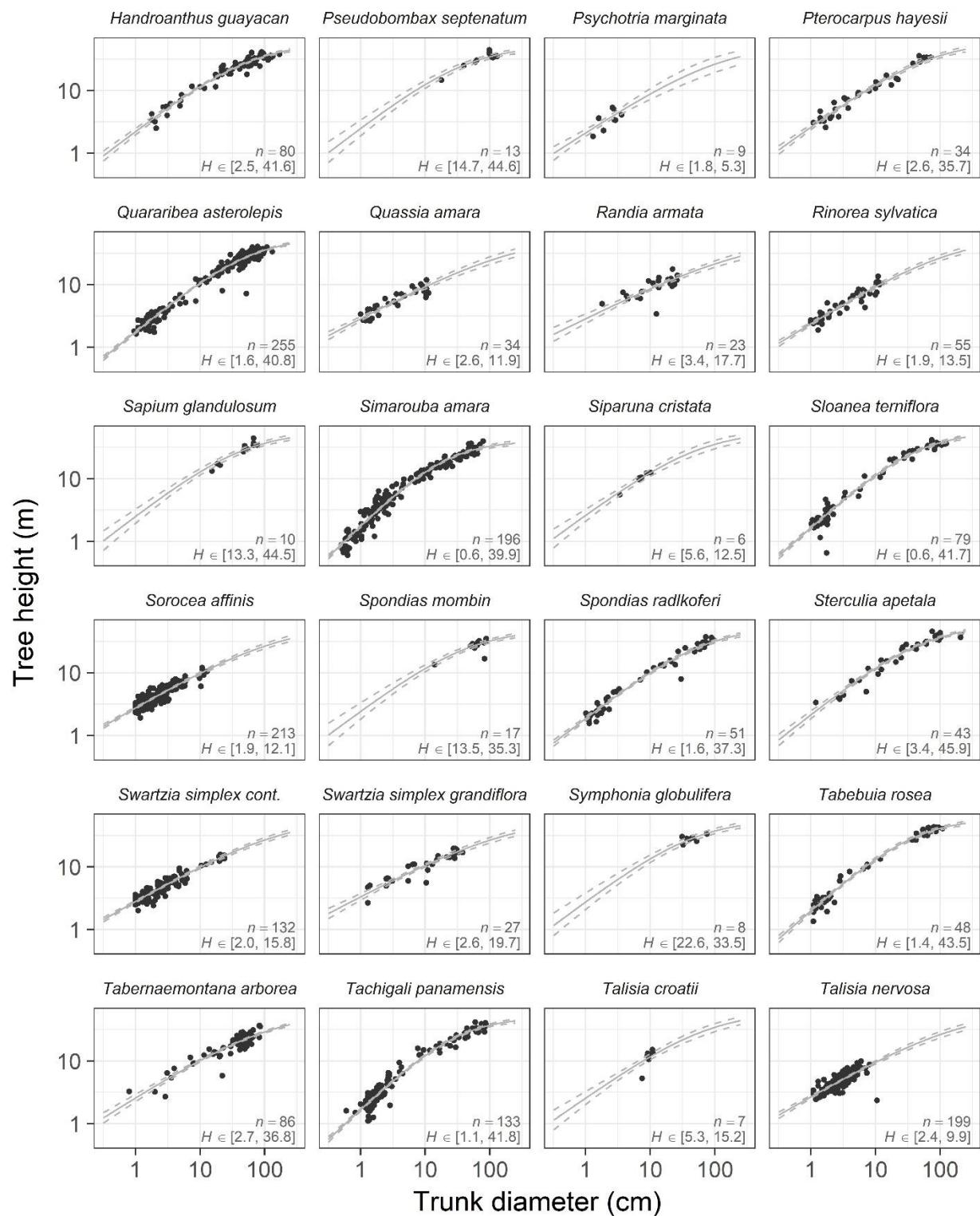


Figure S1. (continued).

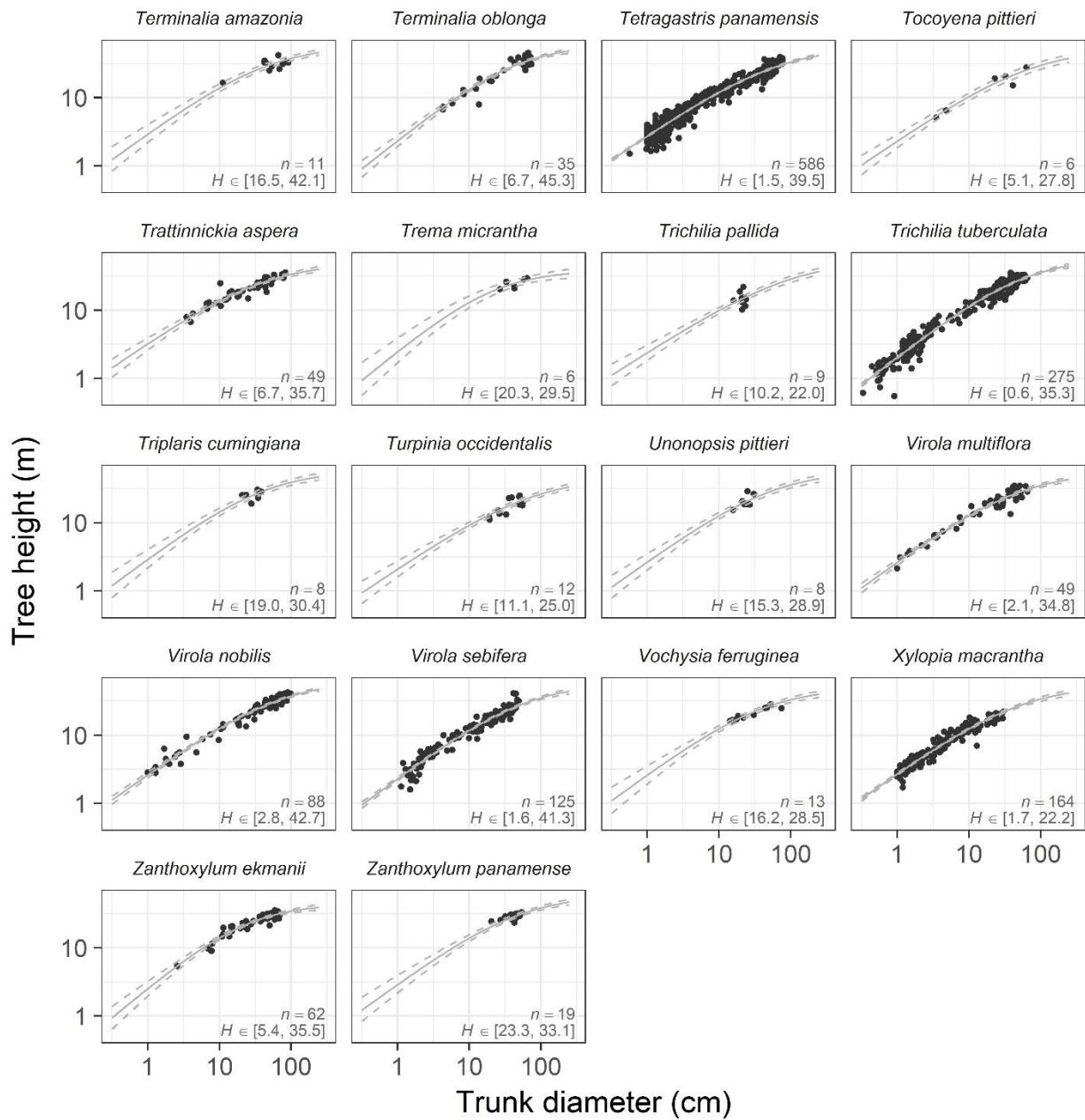


Figure S2. Species-specific relationships of crown area with trunk diameter, showing the data (points) and fitted relationships (solid lines) together with their 90% posterior central intervals (dashed lines). The annotations on each plot detail sample size (n) and the observed crown area (C) range for each species. Note the log–log axes (multiple pages).

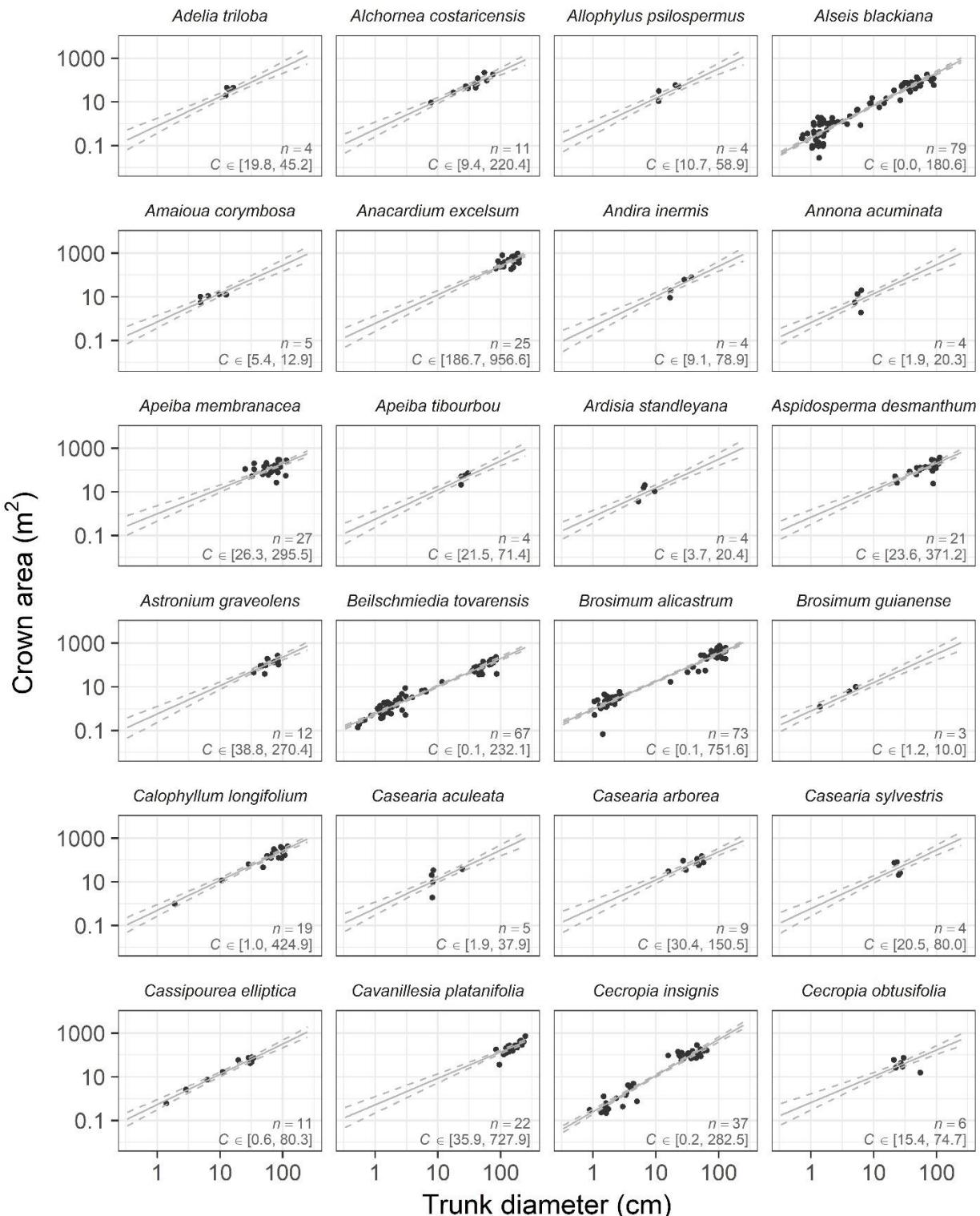


Figure S2. (continued).

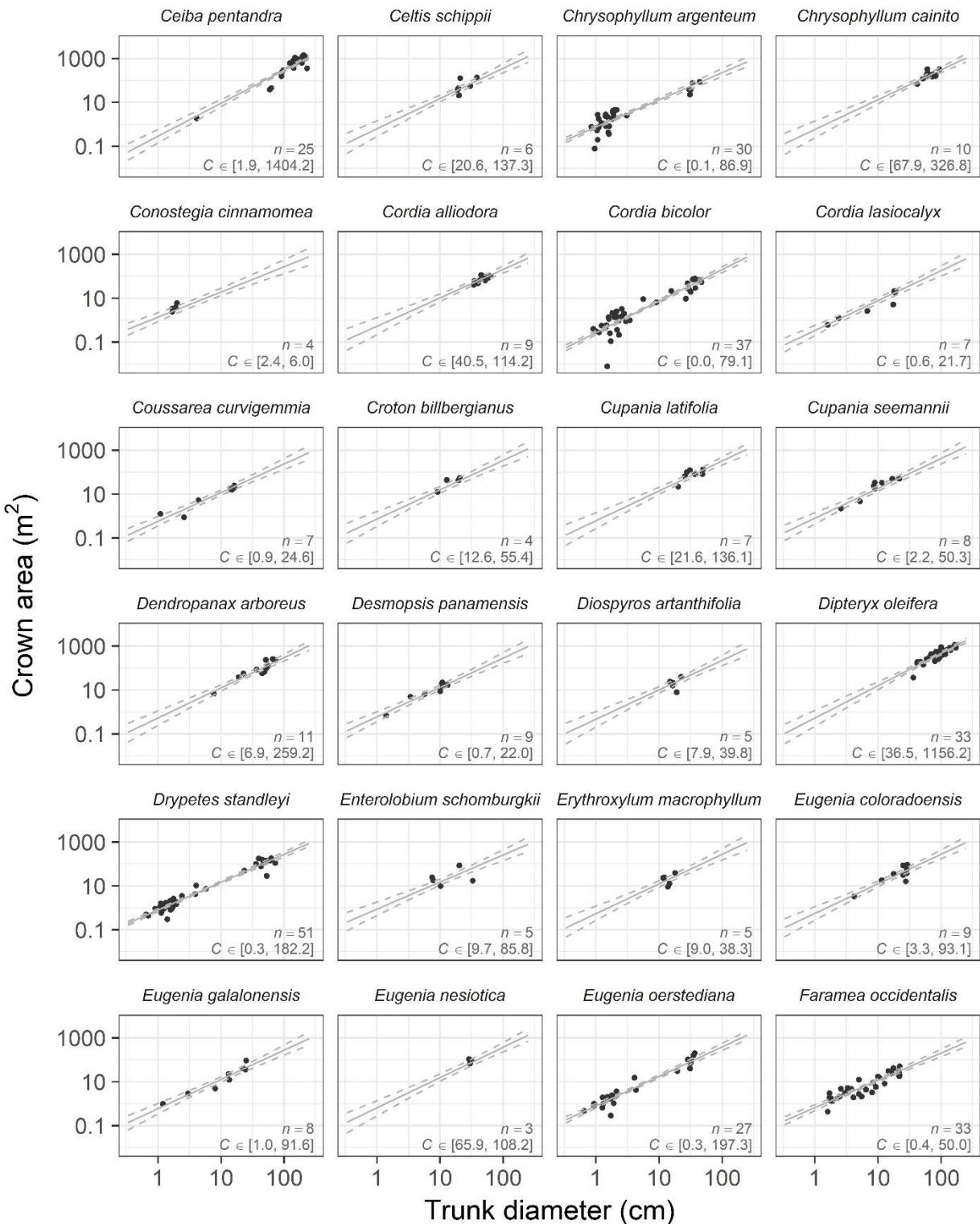


Figure S2. (continued).

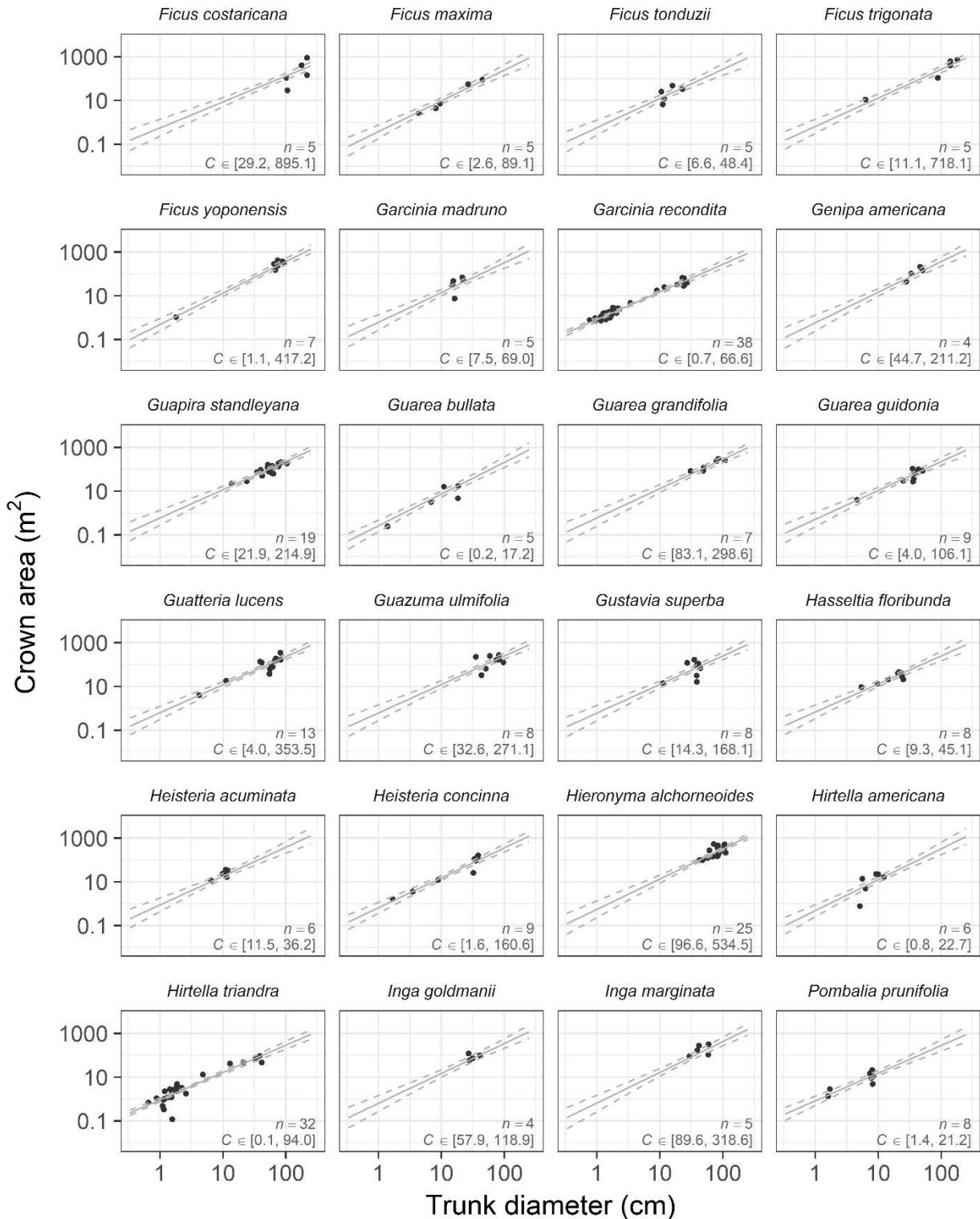


Figure S2. (continued).

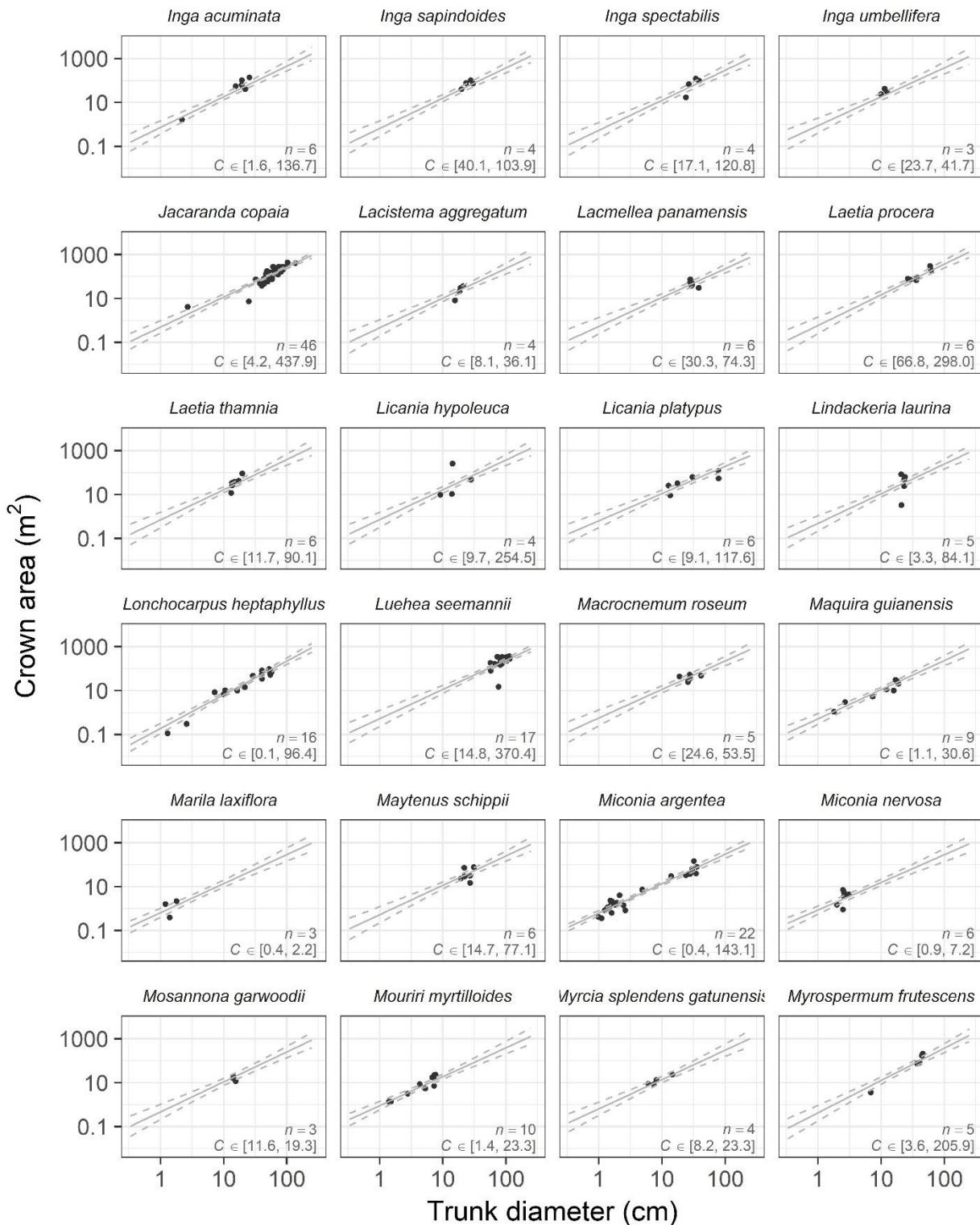


Figure S2. (continued).

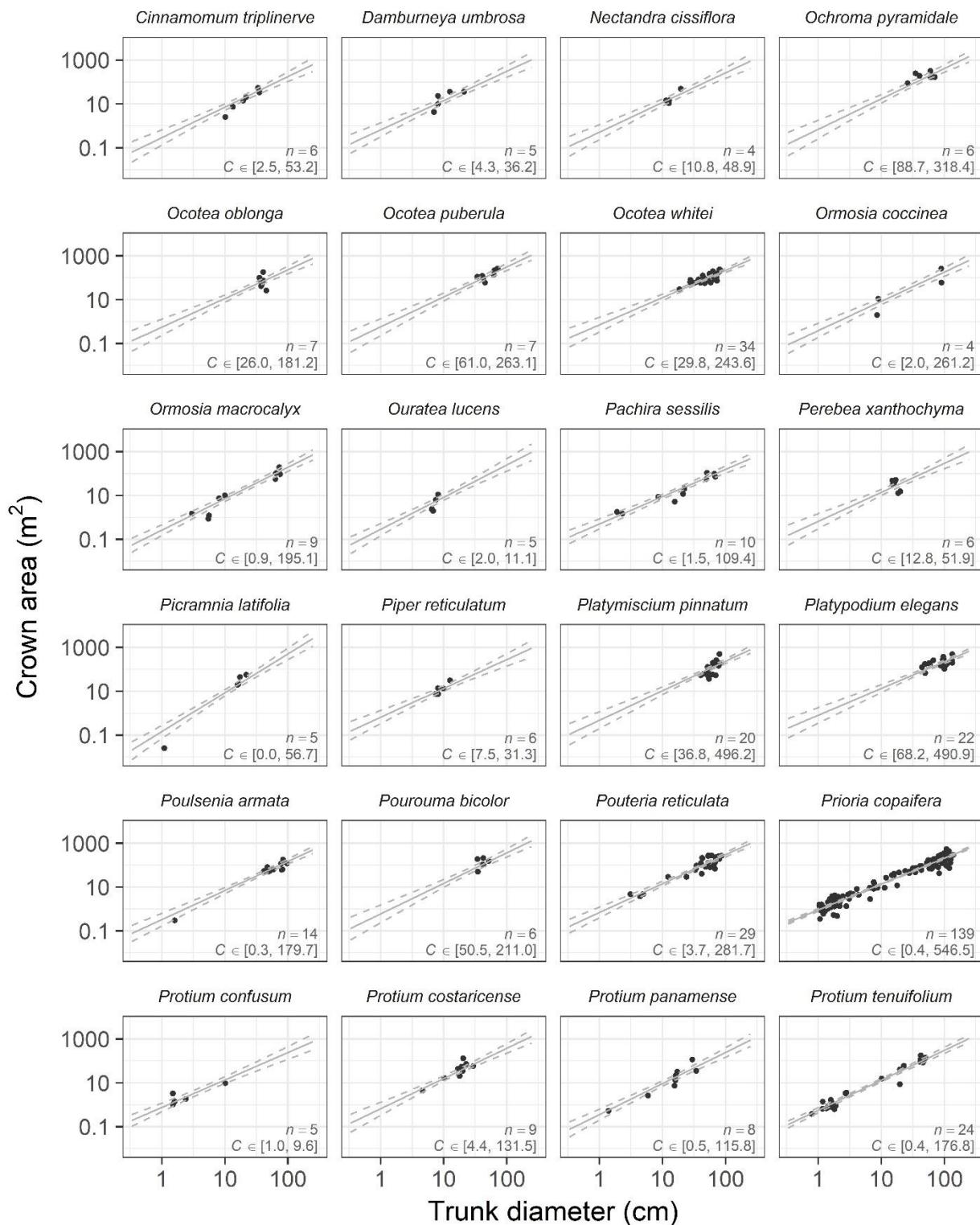


Figure S2. (continued).

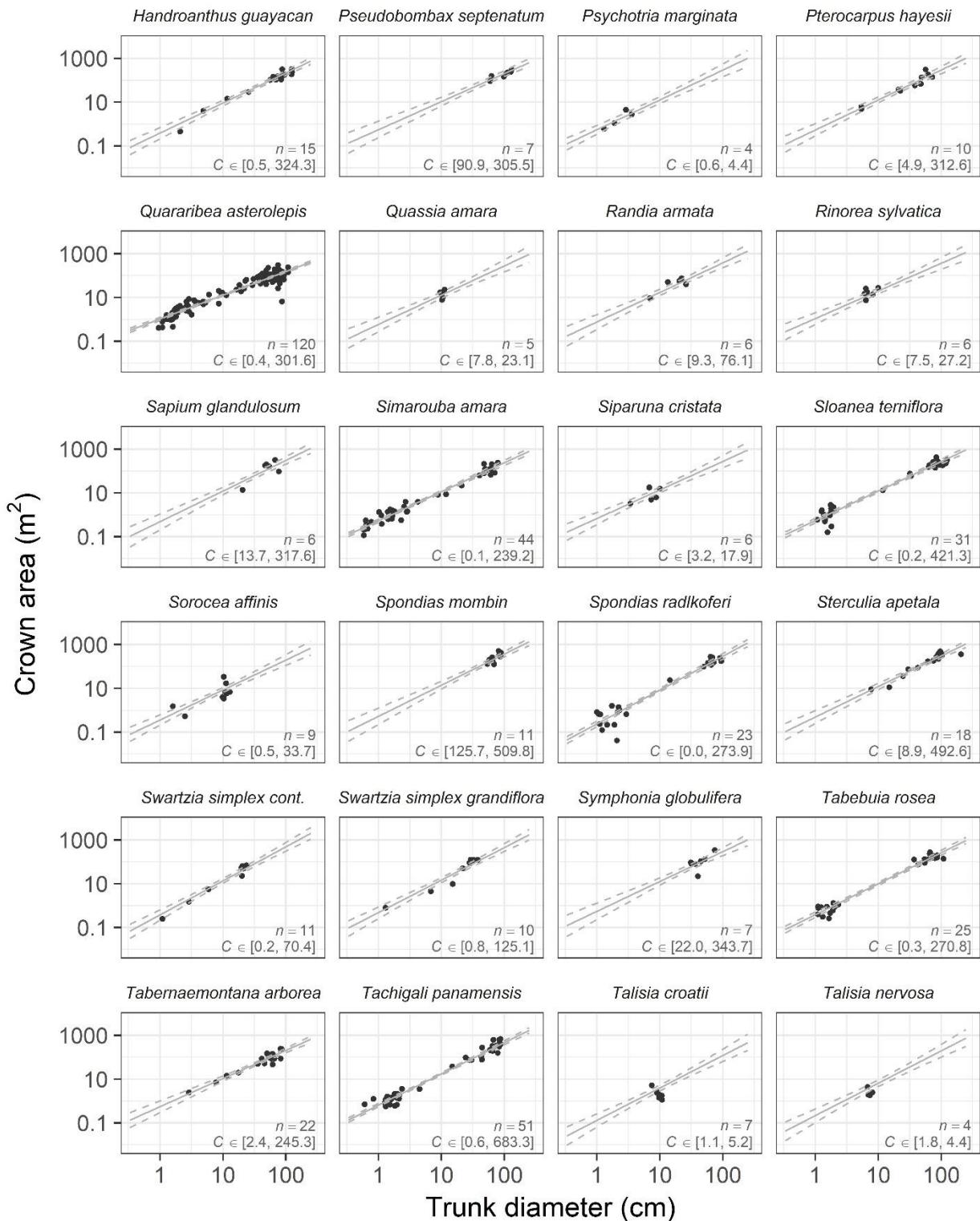


Figure S2. (continued).

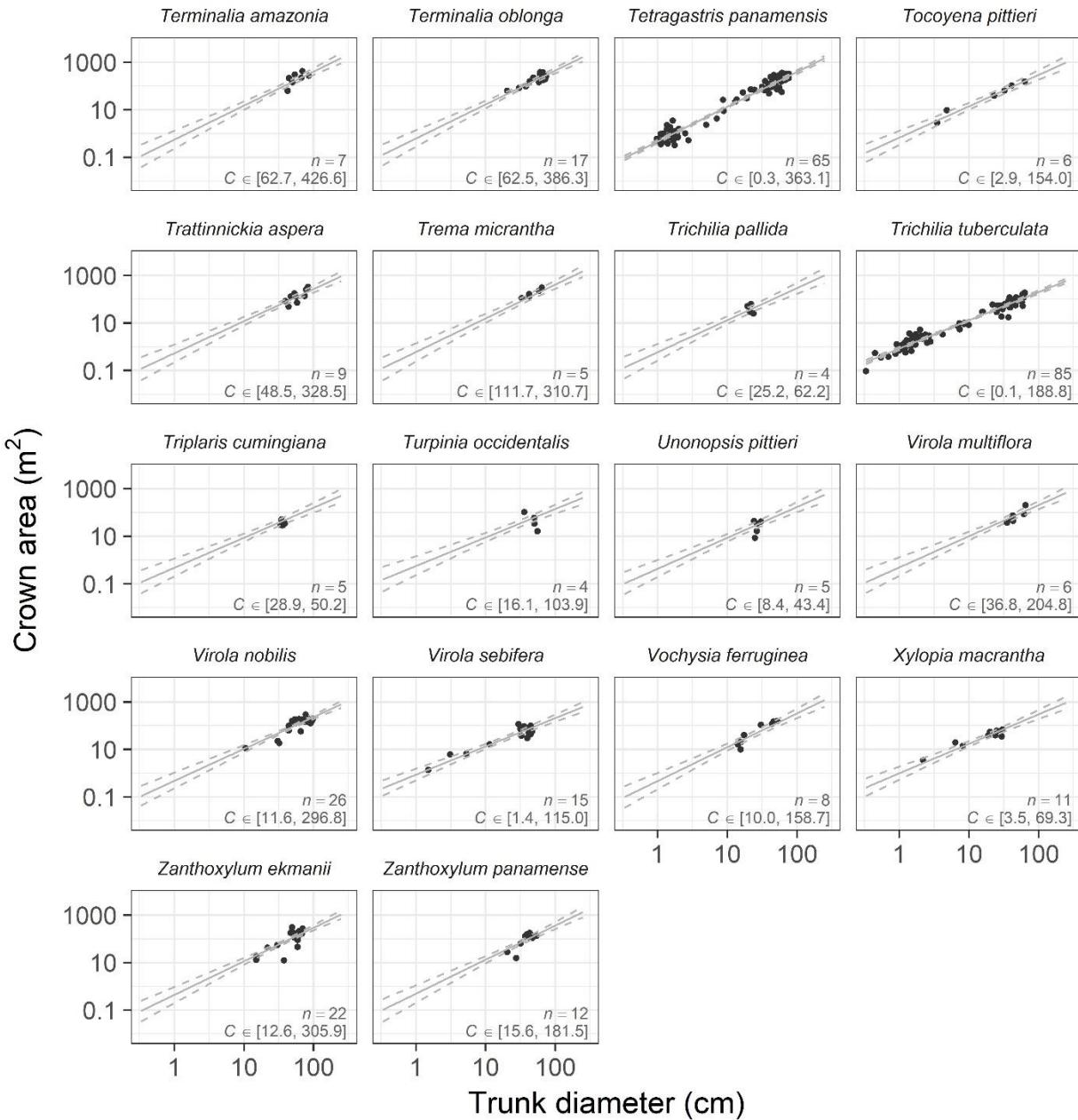
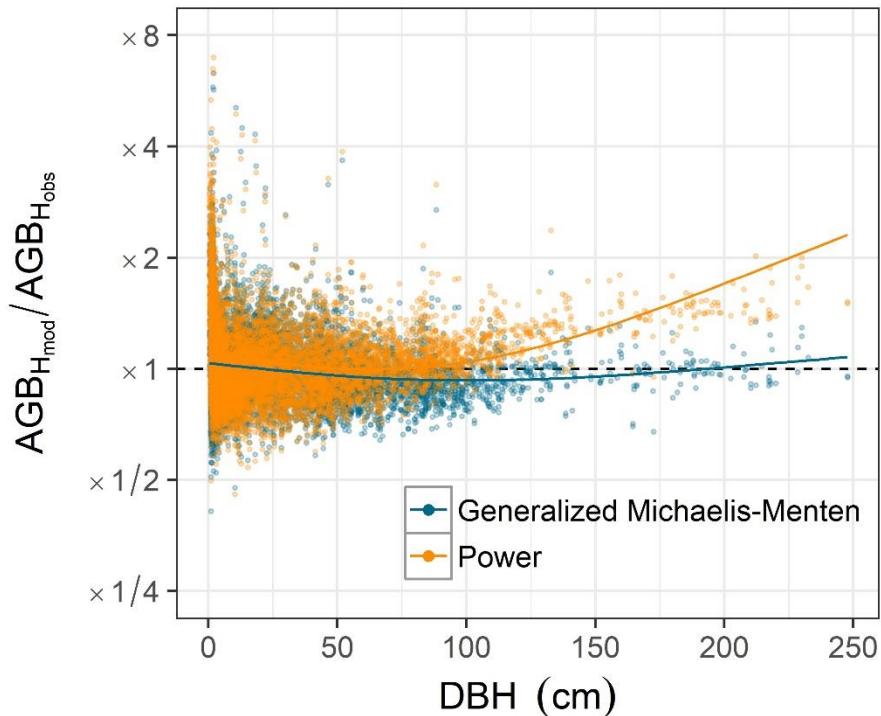


Figure S3. Relative error for estimates of individual tree dry aboveground biomass (AGB , Kg dry matter) based on model predictions of tree height (AGB_{Hmod}) compared with estimates derived from height observations (AGB_{Hobs}). This figure shows the entire range of observed DBHs (Fig. 4b in the main text highlighted differences for large trees, i.e. $DBH > 30$ cm). Modeled tree heights were from community-level models fitted with either the power function (orange dots) or generalized Michaelis-Menten function (blue dots). All AGB estimates were based on the biomass allometry equation 6 (from Chave et al. 2014) and used the average value of wood density across species, to highlight variation related to the height allometry. The lines are LOESS smoothers that illustrate the overall departures of each model from perfect prediction (i.e. AGB_{Hmod}/AGB_{Hobs} ratio equal to unity) as a function of DBH.



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Section S2: Stan code

Power function model

```
// Linear mixed model with varying parameters among species and one species level covariate
// for a power function allometric model
data {
    // inputs
    int<lower=0> N; // number of individuals
    int<lower=0> Ng; // number of species
    int<lower=0> p; // number of parameters per species  vector[N] y; // dependent variable: natural
logarithm of tree height or crown area
    vector[N] x; // independent variable: natural logarithm of trunk diameter
    int g[N]; // species indicator
    real xbar; // mean of x  vector[Ng] z; // trait covariate, one value per species
    real zbar; real zs; // mean and standard deviation of the covariate z across species
}
transformed data{
    vector[Ng] zc; // centered and scaled covariate
    for ( i in 1:Ng )
    {
        zc[i] = ( z[i] - zbar ) / zs;
    }
}
parameters {
    vector[p] theta[Ng]; // species parameters of the allometric model: here a and b (Eq. 1 in the main
text)
    vector[p] alpha; // community level means (means of parameters across species) (Eq. 5 of the main text)
    vector[p] beta; // community level effects of the covariate 'z' on each parameter (Eq. 5 of the main
text)
    real<lower=0> sigmaa; // standard deviation of parameter a across species,
    real<lower=0> sigmab; // standard deviation of parameter b across species
    real<lower=0> serror; // standard deviation for observation error (sigmav in Eq. 1 of main text)
}
transformed parameters {
    vector[N] y_hat; // predicted mean for each y  for ( n in 1:N )
    {
        // power function
        y_hat[n] = theta[g[n], 1] + theta[g[n], 2] * ( x[n] - xbar );
    }
}
model {
    // prior distributions for the community level means
    alpha[1] ~ normal( 0, 100 ); alpha[2] ~ normal( 0, 100 );
    // prior distributions for community level covariate effects
    beta[1] ~ normal( 0, 100 ); beta[2] ~ normal( 0, 100 );
    // community level parameters act as priors of species level parameters
    for ( i in 1:Ng )
    {
        theta[i, 1] ~ normal( alpha[1] + beta[1] * zc[i], sigmaa ); // prior for species level parameter Log a
        theta[i, 2] ~ normal( alpha[2] + beta[2] * zc[i], sigmab ); // prior for species level parameter b
    }
    // data model
    y ~ normal( y_hat, serror );
    // weakly informative priors for scale parameters
    sigmaa ~ cauchy( 0.0, 2.5 ); sigmab ~ cauchy( 0.0, 2.5 );
    serror ~ cauchy( 0.0, 2.5 );
}
generated quantities {
    // pointwise log-Likelihoods for WAIC estimation
    vector[N] log_lik;
    for ( n in 1:N )
    {
        log_lik[n] = normal_lpdf( y[n] | y_hat[n], serror );
    }
}
```

Generalized Michaelis-Menten model

```
// Nonlinear mixed model with varying parameters among species and one species level covariate
// for a generalized Michaelis Menten allometric model
data {
    int<lower=0> N; // number of individuals
    int<lower=0> Ng; // number of species
    int<lower=0> p; // number of parameters per species
    vector[N] y; // dependent variable: natural logarithm of tree height or crown area
    vector[N] x; // independent variable: natural logarithm of trunk diameter
    int g[N]; // species indicator
    real xbar; // mean of x
    vector[Ng] z; // trait covariate, one value per species
    real zbar; real zs; // mean and standard deviation of the covariate z across species
}
transformed data{
    vector[Ng] zc; // centered and scaled covariate
    for ( i in 1 : Ng )
    {
        zc[i] = ( z[i] - zbar ) / zs;
    }
}
parameters {
    vector[p] theta[Ng]; // species parameters of the allometric model: here a, b and k (Eq. 1 in the main text)
    vector[p] alpha; // community level means (means of parameters across species) (Eq. 5 of the main text)
    vector[p] beta; // community level effects of the covariate 'z' on each parameter (Eq. 5 of the main text)
    real< lower=0 > sigmaa; // standard deviation of parameter a across species,
    real< lower=0 > sigmab; // standard deviation of parameter b across species,
    real< lower=0 > sigmak; // standard deviation of parameter k across species
    real< lower=0 > serror; // standard deviation for observation error (sigmav in Eq. 1 of main text)
}
transformed parameters {
    vector[N] y_hat; // predicted mean for each y
    for ( n in 1 : N )
    {
        // generalized Michaelis Menten
        y_hat[n] = theta[g[n], 1] + theta[g[n], 2] * log( x[n] ) - log(theta[g[n], 3] + pow( x[n], theta[g[n], 2] ) );
    }
}
model {
    // prior distributions for the community level means
    alpha[1] ~ normal( 0, 100 ); alpha[2] ~ normal( 0, 100 )T[0,]; alpha[3] ~ normal( 0, 100 )T[0,];
    // prior distribution for community level covariate effects
    beta[1] ~ normal( 0, 100 ); beta[2] ~ normal( 0, 100 ); beta[3] ~ normal( 0, 100 );
    // community level parameters act as priors of species level parameters
    for ( i in 1 : Ng )
    {
        theta[i, 1] ~ normal( mu[1] + theta[1] * zc[i], sigmaa ); // prior for species level parameter log a
        theta[i, 2] ~ normal( mu[2] + theta[2] * zc[i], sigmab )T[0,]; // prior for species level parameter b
        theta[i, 3] ~ normal( mu[3] + theta[3] * zc[i], sigmak )T[0,]; // prior for species level parameter k
    }
    // data model
    y ~ normal( y_hat, serror );
    // weakly informative priors for scale parameters
    sigmaa ~ cauchy( 0.0, 2.5 ); sigmab ~ cauchy( 0.0, 2.5 ); sigmak ~ cauchy( 0.0, 2.5 );
    serror ~ cauchy( 0.0, 2.5 );
}
generated quantities {
    // pointwise log-likelihoods for WAIC estimation
    vector[N] log_lik;
    for ( n in 1 : N )
    {
        log_lik[n] = normal_lpdf( y[n] | y_hat[n], serror );
    }
}
```

Rescaled Weibull model

```
// Nonlinear mixed model with varying parameters among species and one species level covariate
// for a rescaled Weibull allometric model
data {
    int<lower=0> N; // number of individuals
    int<lower=0> Ng; // number of species
    int<lower=0> p; // number of parameters per species  vector[N] y; // dependent variable: natural
logarithm of tree height or crown area
    vector[N] x; // independent variable: natural logarithm of trunk diameter
    int g[N]; // species indicator
    real xbar; // mean of x  vector[Ng] z; // trait covariate, one value per species
    real zbar; real zs; // mean and standard deviation of the covariate z across species
}
transformed data{
    vector[Ng] zc; // centered and scaled covariate
    for ( i in 1 : Ng )
    {
        zc[i] = ( z[i] - zbar ) / zs;
    }
}
parameters {
    vector[p] theta[Ng]; // species parameters of the allometric model: here a, b and k (Eq. 1 in the main
text)
    vector<lower=0>[p] alpha; // community level means (means of parameters across species) (Eq. 5 of the
main text)
    vector[p] beta; // community level effects of the covariate 'z' on each parameter (Eq. 5 of the main
text)
    real<lower=0> sigmaa; // standard deviation of parameter a across species,
    real<lower=0> sigmab; // standard deviation of parameter b across species,
    real<lower=0> sigmak; // standard deviation of parameter k across species
    real<lower=0> serror; // standard deviation for observation error (sigmav in Eq. 1 of main text)
}
transformed parameters {
    vector[N] y_hat; // predicted mean for each y  for ( n in 1 : N )
    {
        // Rescaled Weibull [version with improved numerical stability]
        // http://mc-stan.org/misc/warnings.html#exception-hamiltonian-proposal-rejected
        y_hat[n] = log( theta[g[n], 1] ) + log1m_exp( - theta[g[n], 2] * pow( x[n], theta[g[n], 3] ) );
    }
}
model {
    // prior distribution for the parameters of the regression predicting population level parameters
    alpha[1] ~ normal( 0, 100 )T[0,]; alpha[2] ~ normal( 0, 100 )T[0,]; alpha[3] ~ normal( 0, 100 )T[0,];
    // prior distribution for community level covariate effects
    beta[1] ~ normal( 0, 100 ); beta[2] ~ normal( 0, 100 ); beta[3] ~ normal( 0, 100 );
    // community level parameters act as priors of species level parameters
    for ( i in 1 : Ng )
    {
        theta[i, 1] ~ normal( mu[1] + theta[1] * zc[i], sigmaa )T[0,]; // prior for species level parameter a
        theta[i, 2] ~ normal( mu[2] + theta[2] * zc[i], sigmab )T[0,]; // prior for species level parameter b
        theta[i, 3] ~ normal( mu[3] + theta[3] * zc[i], sigmak )T[0,]; // prior for species level parameter k
    }
    // data model
    y ~ normal( y_hat, serror );

    // weakly informative priors for scale parameters
    sigmaa ~ cauchy( 0.0, 2.5 ); sigmab ~ cauchy( 0.0, 2.5 ); sigmak ~ cauchy( 0.0, 2.5 );
    serror ~ cauchy( 0.0, 2.5 );
}
generated quantities {
    // pointwise log-likelihoods for WAIC estimation
    vector[N] log_lik;
    for ( n in 1 : N )
    {
        log_lik[n] = normal_lpdf( y[n] | y_hat[n], serror );
    }
}
```